

Left-most Derivation

In the left most derivation, the input is scanned and replaced with the production rule from left to right. So in left most derivatives we read the input string from left to right.

Example: Production rules:

1. $S = S + S$
2. $S = S - S$
3. $S = a \mid b \mid c$

Input:

```
a - b + c
```

The left-most derivation is:

1. $S = S + S$
2. $S = S - S + S$
3. $S = a - S + S$
4. $S = a - b + S$
5. $S = a - b + c$

Right-most Derivation

In the right most derivation, the input is scanned and replaced with the production rule from right to left. So in right most derivatives we read the input string from right to left.

Example:

1. $S = S + S$
2. $S = S - S$
3. $S = a \mid b \mid c$

Input:

```
a - b + c
```

The right-most derivation is:

1. $S = S - S$
2. $S = S - S + S$
3. $S = S - S + c$

4. $S = S - b + c$
5. $S = a - b + c$

Parse tree

- Parse tree is the graphical representation of symbol. The symbol can be terminal or non-terminal.
- In parsing, the string is derived using the start symbol. The root of the parse tree is that start symbol.
- It is the graphical representation of symbol that can be terminals or non-terminals.
- Parse tree follows the precedence of operators. The deepest sub-tree traversed first. So, the operator in the parent node has less precedence over the operator in the sub-tree.

The parse tree follows these points:

- All leaf nodes have to be terminals.
- All interior nodes have to be non-terminals.
- In-order traversal gives original input string.

Example:

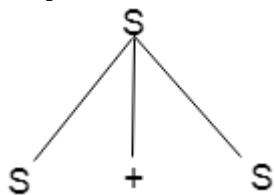
Production rules:

1. $T = T + T \mid T * T$
2. $T = a \mid b \mid c$

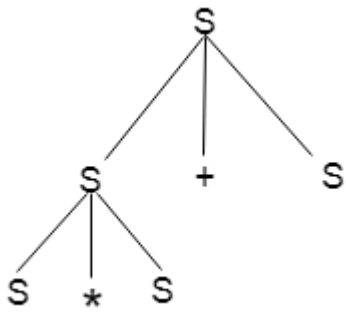
Input:

a * b + c

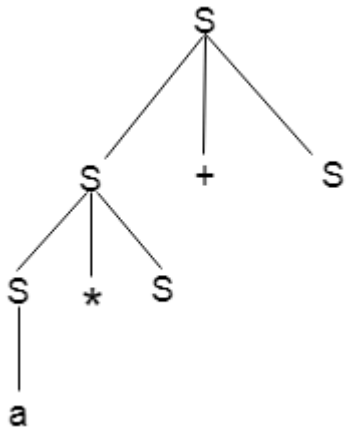
Step 1:



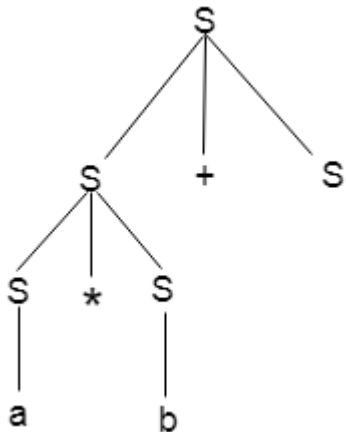
Step 2:



Step 3:



Step 4:



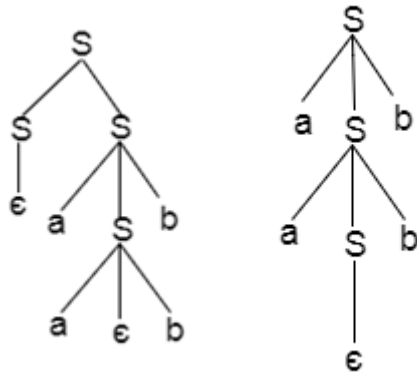
Ambiguity

A grammar is said to be ambiguous if there exists more than one leftmost derivation or more than one rightmost derivative or more than one parse tree for the given input string. If the grammar is not ambiguous then it is called unambiguous.

Example:

1. $S = aSb \mid SS$
2. $S = \epsilon$

For the string aabb, the above grammar generates two parse trees:



If the grammar has ambiguity then it is not good for a compiler construction. No method can automatically detect and remove the ambiguity but you can remove ambiguity by re-writing the whole grammar without ambiguity.

Step 5:

