

SNS COLLEGE OF ENGINEERING **Coimbatore - 641 107**



TOPIC:5 -Pigeon HolePrinciple

Hole principle · Pigeon

If (n+1) pigeon occupies 'n' holes then atleast one hole has more than I pigeon.

Greneralized Pigeon Hole Principle

If 'm' pigeon occupies 'n' holes (m>n), then atteast one hole has more than $\lceil \frac{m-1}{n} \rceil + 1$ pigeon.

1) Show that, among 100 people, atleast 9 of Thun were born in the same month.

Here, No. of pigeon = m = No. of people

No. of Holes = n = No. of month

Then by generalized pigeon hole principle,

$$\left[\frac{m-1}{n}\right]+1 \Rightarrow \left[\frac{100-1}{12}\right]+1 = 8+1$$

-. 9 were born in the same month.



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2) show that, ownoring it seven colours are used to paint 50 bicycles, atleast 8 bicycles will be the same colour.

Here, No. of pigeon = m = No. of bicycle

No. of Holes = n = 7 = No. of colours. Thun by generalized pigeon hole principle,

$$\left[\frac{m\bar{\epsilon}1}{n}\right]+1 \Rightarrow \left[\frac{50\bar{\epsilon}1}{7}\right]+1 \Rightarrow 7+1$$

⇒ 8

: at least 8 bicycles will have the same colour.

3) Prove that in any group of six people. There must be atleast 3 mutual friends or itleast 3 mutual enumies.

Let those six people will be A, B, C, D, E and F. Fix A. The remaining 5 peoples can be accommodate into 2 groups namely

(1) Friends of A and (2) Enemies of A.

Now, by generalized pigeon hole principle, at least one of the group must contain



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 $\left\lceil \frac{m-1}{n} \right\rceil + 1 \Rightarrow \left\lceil \frac{2}{2} \right\rceil + 1 \Rightarrow 3$ Let the group friend of A contain 3 people

case (i)

If any two of these 3 people (B,C,D) are friends, then these two together with A form mutual friends.

case (ii)

If no two of these 3 people are friends, then these 3 people (B, c, D) are multial eneminal entire line either case, we get the required conclusion. If the group of enemises of A contain

3 people, by the above similar argument we get the required conclusion.



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4) What is the maximum number of students required in a discrete mathematics class to b. Sure that atleast six will receive the same grade if there are five possible grades A.B.C, D and E?

No of pigeon hole = No of grades

Let k be number of students (pigeon) in discrete mathematics class.

$$\Rightarrow [K = 5]$$

.. The total number of students = Kn+1

: Minimum number of students = 26