



**Coimbatore - 641 107** 

## **TOPIC: 11 - HARMONIC ANALYSIS**

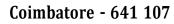
The process of finding the fourier series for a function given by such values of the function and independent variable is known as Harmonic analysis.  $y = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos nx + \sum_{n=1}^{\infty} b_n \sin nx$ where  $a_0 = 2 \left[\frac{ZY}{n}\right]$  $a_n = 2 \left[\frac{ZY \cos nx}{n}\right]$ 





OF	ind	the	series	upto	the	Second	hanmon
x		17	211 3	TT	41	511 3	277
y	[.0		1.9			1.2	1.0
sol		10				1 and the	La Sinax
0-847 b	a	0 = 2	[24]	= 2 ( .	$\left(\frac{8\cdot7}{6}\right) = 2$	bi Bina +1	.9
	c	$n_1 = 2$	[Zy cosa	7 = 2 (	(=++) =	-0.2001	
	-	a2 =	2/zya	262 x 7 =	$= 2\left(\frac{-0}{6}\right)$	3)=-0.1	
		6,2	2 (245	<u>ina</u> 7 =	2 ( 0.	$\frac{5196}{6} = 0.$	1732
		b2 =	2[ 243	in2x ]	= 2(-0	$\frac{173^2}{6} = $	-0.0577
9	Sub	the	re valu	- Cal	7 + (-0	1.1) Corza	
	Y=	2.7	+ 60.36	+(0	.1732) 5	nina -10.0	sins (דדז







ysinez	0		6212.01	1-7	0	42	- 1.292	ġ	0.1737
4003231	1 .	- 0.7		-0.45	-0.75	8.1	9.0-	1	- 0.3
x nist y	0	1.2124	1. 6400		- 1-299	0.02	-1.0392	0	0.6196
yeasa	-	2.0	-0.95	1.4	-0.75	2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.0	1	-1.1
Sinex	0	+ 0.866	- 0.866	0	0.846		TO . \$ 06	0	
Cosez	1	-0.5	-0.5	7	-0.5	40.01	MY	- 6	0
Sinz	0	0 = 866	0.866	0	-0.866	-0.866	9	0	
Cosx	-	0.5	10.7	1	-0.5	0.5		-	



**Coimbatore - 641 107** 



2. Compute first two harmonic of the fourier Series of first two harmonic of the fourier  $\frac{3}{2}$  of f(x) from the table below.  $\frac{3}{2}$  of  $\frac{7}{5}$   $\frac{7}{3}$   $\frac{7}{2}$   $\frac{27}{3}$   $\frac{57}{6}$   $\frac{7}{7}$  $\frac{9}{198}$  1.3 1.05 1.8 -0.88 -0.25 1.98

sol:

 $\theta = \frac{2\pi x}{T}$  $a_0 = 2\left[\frac{24}{n}\right] = 2\left[\frac{4.5}{6}\right] = 1.5$  $a_1 = 2 \int \frac{5y \cos \theta}{n} \int = 2 \left[ \frac{1.12}{6} \right] = 0.3733$  $a_2 = 2 \left[ \frac{2 y \cos 2\theta}{h} \right] = 2 \left[ \frac{2.67}{b} \right] = 0.8900$  $b_1 = 2 \left[ \frac{2.4 \sin \theta}{n} \right] = 2 \left[ \frac{3.0137}{6} \right] = 1.004 b$  $b_2 = 2 \left[ \frac{2y \sin 2\theta}{6} \right] = 2 \left[ \frac{-0.3291}{6} \right]$ =-0.1097 Sub all these values in (). y= 1.57 (0.3733) costo+ (0.8900) cose 0 + (1.0046) dimo + (-0.1097) &in20





	•	MATORIC					www.sn	sgroups.com
A SINES	6	2	1.1258	~ 0.0%	0	-0.762	0.216.	Segroups.com
y cose	1. 4.0	81.1	0.65	- 0.525	1.3	60 44	6-)2S	2. b7
y sing	1	0	1,1258 -0.65	. 0.9693	0	0.846 + 0.44 0.7421	0.2165	3.0137
grosp	>	86.1	0.65	-0.525	-1-3	44.04	-0.125	1.12
ginzo	-	0	998.0	-0.8 66	9	0.866	-0.446	
Cos2B		æ	5.0-	- 0.5	5-12	5.0	ed .	
QinB		0	0.8660	0.2660	Q	-0.866	-0.846	
0.00		1 In	0.2	- 0.5	-j- <b>t</b> -	- 0.5	0.5	- 2
	20	1.98	1.3	1.05	1.3	All (240) -0.86	51(50) -0.25	4.5
	St B	C	3 (to)	$\frac{2\pi}{3}(w)$	(1) (140)	H. (240)	<u>511</u> (300)	





(3) Find the Fourier series as far as the second  
harmonic to represent the function given in the  
following data:  

$$\frac{x}{d(x)} \frac{0}{q} \frac{1}{18} \frac{2}{24} \frac{8}{28} \frac{1}{24} \frac{5}{28} \frac{1}{24} \frac{5}{28}$$

$$\frac{x}{d(x)} \frac{1}{q} \frac{2}{18} \frac{2}{24} \frac{2}{28} \frac{1}{24} \frac{5}{28} \frac{5}{24} \frac{5}{28}$$

$$\frac{x}{d(x)} \frac{1}{q} \frac{1}{18} \frac{2}{24} \frac{2}{28} \frac{1}{24} \frac{5}{28} \frac{5}{24} \frac{5}{28} \frac{5}{28}$$

$$\frac{x}{d(x)} \frac{1}{q} \frac{1}{18} \frac{2}{24} \frac{1}{28} \frac{1}{28} \frac{1}{24} \frac{5}{28} \frac{5}{24} \frac{5}{28} \frac{5}{28} \frac{5}{24} \frac{5}{28} \frac{5}{28} \frac{5}{28} \frac{5}{28} \frac{1}{28} \frac{5}{28} \frac{5}{28} \frac{5}{28} \frac{1}{28} \frac{5}{28} \frac{5$$





