



POWER SYSTEM ANALYSIS

UNIT - I

PERMANENT MAGNET BRUSHLESS DC MOTOR

CLASSIFICATION of PMBLDC motor.

PMBLDC motor is classified on the basis of flux density distribution in the air gap of the motor.

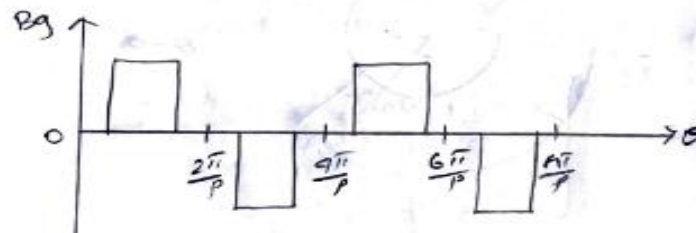
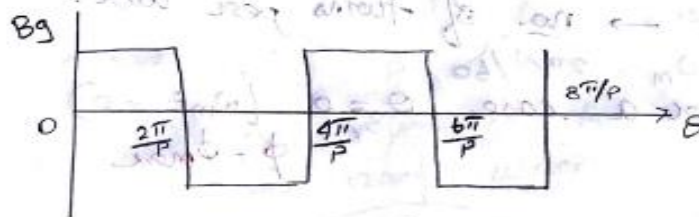
They are

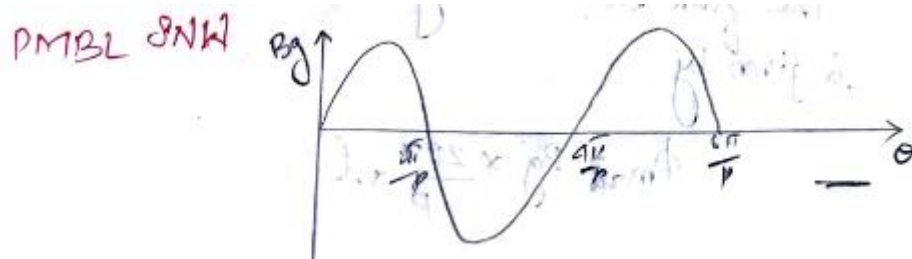
- * PMBL square wave DC motor.
- * PMBL (SIN) motor (sine wave).

PMBL square wave DC motor.

Two types

- * 180° pole arc PMBL SQW dc motor
- * 120° pole arc PMBL SQW dc motor.





EMF equation for PMBL & N/A DC motor

The basic emf equation results to
Conventional DC motor.

Let us assume that,

$P \rightarrow$ No. of poles

$B_g \rightarrow$ flux density in the airgap of the motor (Wb/m^2)

B_g is assumed to be constant throughout entire airgap

$r \rightarrow$ radius of the airgap (in m)

$l \rightarrow$ length of the armature (in m)

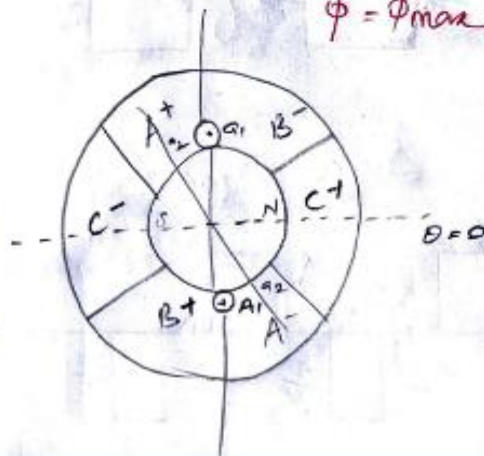
$\omega_m \rightarrow$ angular velocity in mech. rad/sec

$T_c \rightarrow$ no. of turns per coil.

$$\omega_m = \frac{2\pi N}{60}$$

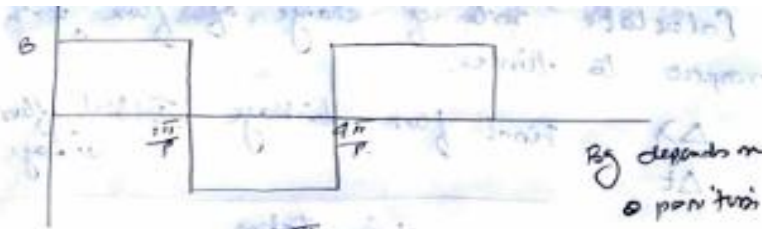
Consider a case $\theta = 0$ ($\omega_m t = 0$)

$$\phi = \phi_{\max}$$



The flux enclosed by the coil per pole is given by

$$\phi_{max} = B_g \times \left(\frac{2\pi r l}{p} \right) \times \text{Area}$$



$$\begin{aligned} \phi_{max} &= r l \int_0^{\pi} B_g(\theta) d\theta \\ &= B_g r l [\theta]_0^{\pi} \end{aligned}$$

$$\boxed{\phi_{max} = B_g r l \pi}$$

The same condition, the flux linkage of the coil is, flux linkage = $\phi \times \text{turns}$

$$\lambda_{max} = \left(B_g \frac{2\pi r l}{p} \right) \cdot T_c \quad \text{wb-Turns}$$

Let us consider rotor rotated in counter clockwise direction and when $\omega t = \frac{\pi}{2}$ (90°)

The flux enclosed by the coil is $\phi = 0$
flux linkage $\lambda = 0$

The flux linkage of the coil varies with rotor position θ .

The flux linkage of coil changes from maximum value.

$$\boxed{B_g \cdot \frac{2\pi r l}{p} \cdot T_c} \quad \text{at } \omega t = 0 \quad \text{to} \quad \boxed{\text{Zero}}$$

$$\text{at } t = \frac{\pi}{\omega} \quad \text{time } \frac{\pi}{\omega} \text{ms}$$

Calculate rate of change of flux linkage with respect to time.

$$\frac{\Delta \lambda}{\Delta t} = \frac{\text{Final flux linkage} - \text{Initial flux linkage}}{\text{Time taken}}$$

$$= \frac{0 - B_g \cdot \frac{2\pi r l \tau_c}{P}}{\pi / \omega_m}$$

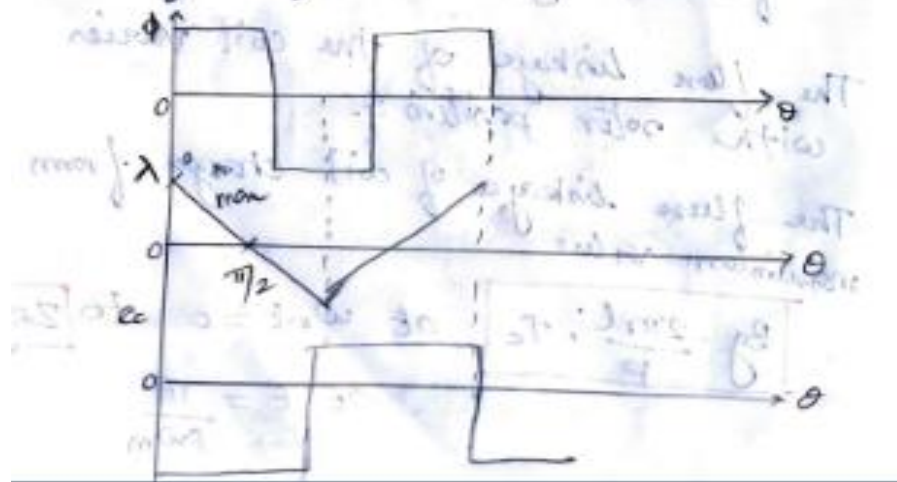
$$\frac{\Delta \lambda}{\Delta t} = -2B_g r l \tau_c \omega_m$$

The EMF induced in coil can be determined using **Electromagnetic induction law**

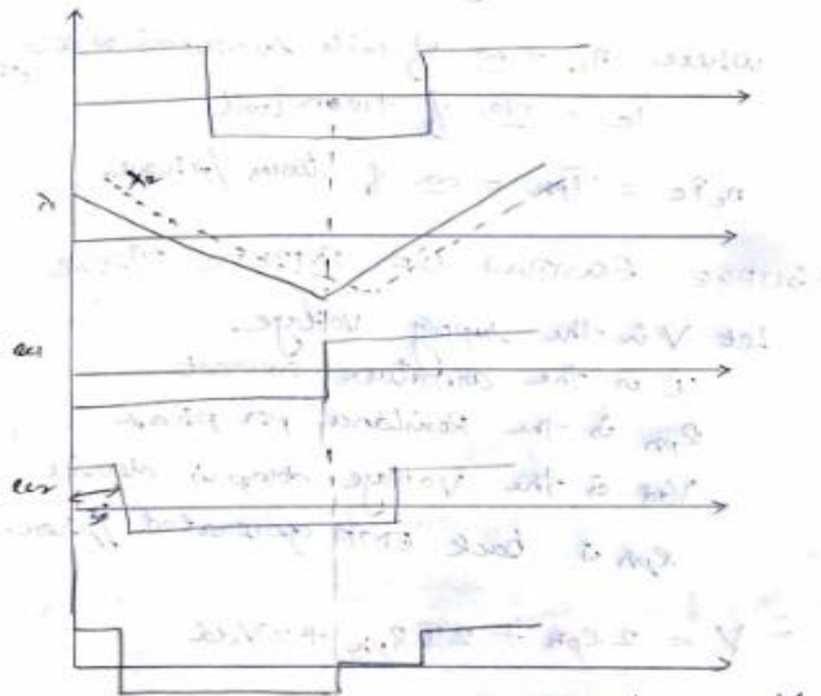
$$e_c = - \frac{d\lambda}{dt} = 2B_g r l \tau_c \omega_m$$

(emf induced in coil)

This emf is for single coil



Consider two coils $A_1 a_1$ and $A_2 a_2$
 The angle b/w two coils 30°



The magnitude of EMF induced in coil $A_1 a_1$ is

$$e_1 = 2 B_g r l T_c \omega_m \text{ Volts}$$

The magnitude of EMF induced in coil $A_2 a_2$ is

$$e_2 = 2 B_g r l T_c \omega_m$$

The sum of 2 coil voltages.

$$e_1 + e_2 = 4 B_g r l T_c \omega_m \text{ Volts}$$

Resultant emf when all coils are connected in series.

$$E_{ph} = 2 B \rho \omega T_{ph} \text{ Volts}$$

where $n_c = \text{no. of coils connected in series}$

$$i_c = \text{no. of turns/coil}$$

$$n_c i_c = T_{ph} = \text{no. of turns/phase}$$

VOLTAGE EQUATION OF PMSM MOTOR

Let V is the supply voltage

I is the armature current

R_{ph} is the resistance per phase

V_{dd} is the voltage drop in device

E_{ph} is back EMF generated / phase

$$V = 2E_{ph} + 2IR_{ph} + 2V_{dd} \text{ negligible}$$

$$I = \frac{V - 2E_{ph}}{2R_{ph}} = \frac{V - E}{R}$$