

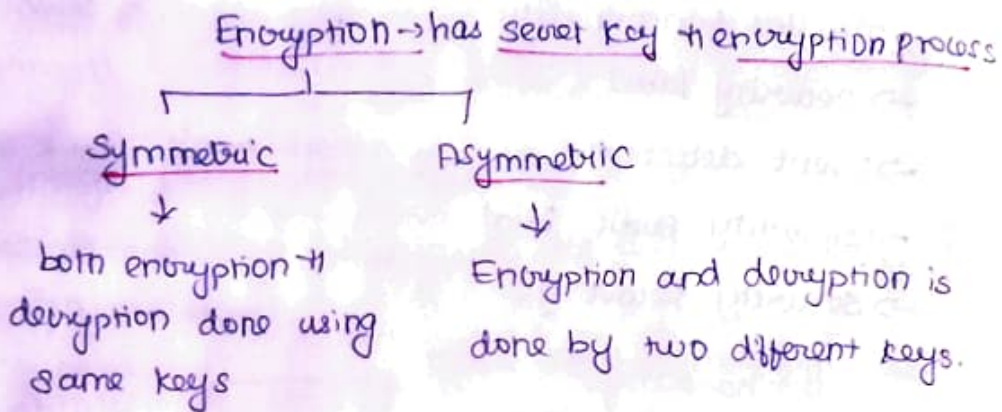
CLASSICAL ENCRYPTION TECHNIQUES

Cryptography :-

Process of converting plain text to cipher text.

→ encrypting. Reverse process is called - decrypting.

Study of encryption techniques - Cryptography.



Attack on encryption

- ↓ → breaking of code.
- Cryptanalysis → Reveals properties of encryp. algo.
 - Brute force attack → Trying all possible keys.

Transposition cipher :-

→ Substitutes text into cipher text.

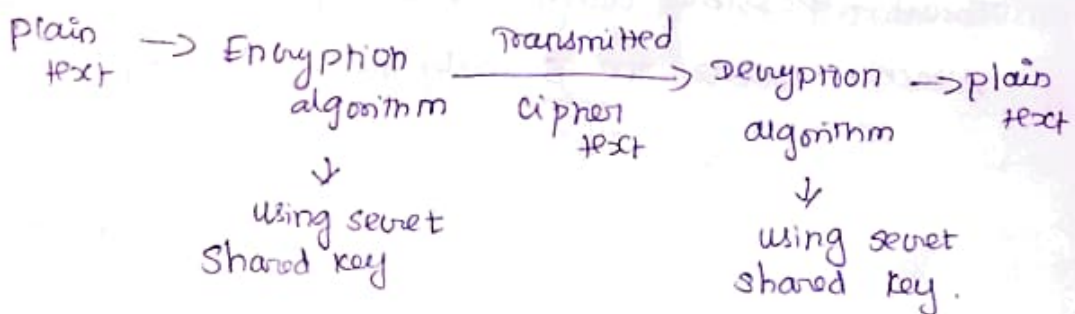
Rotor machines :-

HW device which performs substitution ciphers.

Steganography :-

hiding secret message into image.

Conventional Encryption.



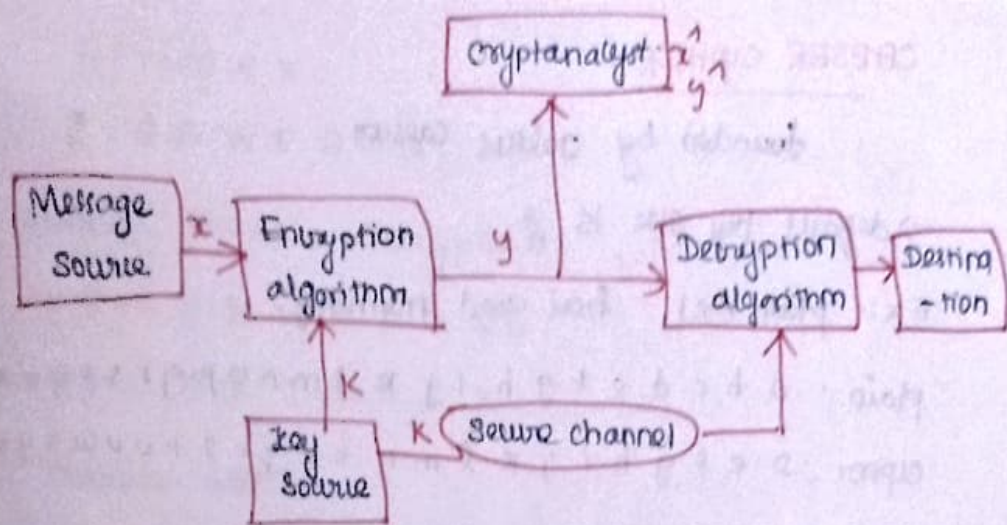


Fig.: Conventional cryptosystem.

2 dimensions of cryptography:

- > transforming plain text to cipher text
- > Numbers of keys used
- > way in which plaintext is processed.

↓
Block cipher - one block at a time

Stream cipher - takes 1/p element continuously

Types of attacks:

- > cipher text only → En. algo
- > known plaintext → one or more plain text, cipher text pair
- > chosen plaintext → plaintext by cryptanalyst, secret key
- > chosen ciphertext → ciphertext by cryptanalyst
- > chosen text → Both encrypted and decrypted text

SUBSTITUTION TECHNIQUES:

A substitution technique is one in which the letters of plaintext are replaced by other letters or by numbers or by symbols.

↓
Encryption is unconditionally secure when cipher text is strong enough which cannot be predicted.

- > Computation secure. → when cost of breaking exceeds value + lifetime of cipher text.

CAESER CIPHER:

founded by Julius Caesar.

→ default key size is 3.

Ex: plain text hai good morning.

plain: a b c d e f g h i j k l m n o p q r s t u v w x y z

cipher: D e f g h i j k l m n o p q r s t u v w x y z

a to z = 0 to 25 number equivalent.

Algorithm:

$$C = E(p, k) = (p + k) \bmod 26 \quad P = E(c, -k) \bmod 26$$

but it can be any key between 1 to 25.

25 keys are possible for brute force attack.

MONO ALPHABETIC CIPHER

Since there is no security for caesar cipher.

Playfair cipher:

Multiple letter encryption.

mono alphabetic example:

↓

It is a substitution cipher in which for a given key the cipher alphabet for each plain alphabet is fixed.

Ex: P is replaced by A means - Its for all occurrence in the plain text.

If key = 3, then $3! = 6$ combinations are possible.

Ex: PT = NETWORK

key = hello how are you.

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

h e l l o w a r y u a b c d e f g h i j k l m n o p q r s t u v w x y z

NETWORK.

g. SBWE DGD

Reverse process - Decryption.

CT - SBWE DGD

PT - NETWORK.

Possible attacks

One A is replaced by E, means every occurrence is replaced by E.

PLAYFAIR CIPHER:

This is the best known multiple letter encryption and treats plaintext as single units and translates the units into ciphertext diagrams.

-> Based on 5x5 matrices using keywords.

Rules: Ex: occurrence.

-> No repeating letters eg: occur

-> create a table.

↳ either left to right or top to bottom
↳ I/J should be in same box.

PT - tall trees

keyword: occurrence.

O	C	U	R	E
N	A	B	D	F
G	H	I	K	L
M	P	Q	S	T
V	W	X	Y	Z

Prepare message:

→ split the pt into plain text

→ If there is duplication of letters by separating by 'x'.

→ If there is odd number of letters, add 'x' at end.

Tall trees → Ta lx lt re es.

This can be done - same pair means have to insert 'x'.

O	C	U	R	E
N	A	B	P	F
G	H	I/J	K	L
M	P	Q	S	T
V	W	X	Y	Z

Ta = pF rule 3

Lx - IZ

lt - tZ rule 1

re - eO rule wrap round

es - RT

CT - PFIZTZEORT.

Ad:

→ It difficult to particular diagram

→ freq analysis is very difficult.

Disad:

→ Easy to break

→ Sufficient No of ciphertext is small.

Hill Cipher:

Developed by mathematician Lester Hill 1929.

Basic mode calculation:

$$21 \text{ mod } 26 \quad 26 \overline{) 21} \quad \text{have to take remainder } 1.$$

Inverse of mod operation:

1) $9^{-1} \text{ mod } 26$

$9x \text{ mod } 26 = 1 \rightarrow$ have to do get 1 as remainder.

$$9 \times 1 \text{ mod } 26 = 9 \text{ mod } 26 = 9$$

$$9 \times 2 \text{ mod } 26 = 18 \text{ mod } 26 = 18$$

$$9 \times 3 \text{ mod } 26 = 27 \text{ mod } 26 = 1$$

$$\text{hence } 9^{-1} \text{ mod } 26 = 3.$$

Similarly $444^{-1} \text{ mod } 26 = 11.$

$$441 \times 25 \text{ mod } 26 = 1$$

$$\text{hence } 441^{-1} \text{ mod } 26 = 25$$

Hill cipher:

Plain Text = HELP

$$\text{key } K = \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix}$$

$$\text{Cipher text } C = K P \text{ mod } 26$$

Split the plain text into two-two letters. as 'HE' 'LP'

$$P = HE = \begin{bmatrix} 7 \\ 4 \end{bmatrix} \rightarrow \text{as 7 and 4 are numbers to H and E.}$$

$$\text{hence } C = \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 7 \\ 4 \end{bmatrix} \text{ mod } 26$$

$$= \begin{bmatrix} 21 & 12 \\ 14 & 20 \end{bmatrix} \text{ mod } 26 \text{ have to add}$$

$$\begin{bmatrix} 3 & 8 \\ 9 & 4 \end{bmatrix} \text{ mod } 26$$

$$\Rightarrow \begin{bmatrix} 3 & 3 \\ 9 & 4 \end{bmatrix} \text{ mod } 26$$

$$\Rightarrow \begin{bmatrix} 7 \\ 8 \end{bmatrix} \Rightarrow \begin{bmatrix} H \\ I \end{bmatrix}$$

Next $P = LP = \begin{bmatrix} 11 \\ 15 \end{bmatrix}$

$$C = KP \text{ mod } 26$$

$$= \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 11 \\ 15 \end{bmatrix} \text{ mod } 26$$

$$= \begin{bmatrix} 33 & 45 \\ 22 & 75 \end{bmatrix} \text{ mod } 26$$

$$= \begin{bmatrix} 7 & 19 \\ 9 & 1 \end{bmatrix} \text{ mod } 26$$

$$= \begin{bmatrix} 0 \\ 19 \end{bmatrix} = \begin{bmatrix} H \\ T \end{bmatrix}$$

Hence **Cipher text: HELP = HIAT**

Decryption:-

Plain text $P \xrightarrow{K^{-1}} KC \text{ mod } 26$

$$K^{-1} = \frac{1}{|K|} \text{adj } K$$

$$|K| = \begin{vmatrix} 3 & 3 \\ 2 & 5 \end{vmatrix} = 15 - 6 = 9 \quad \text{adj } K = \begin{bmatrix} 5 & -3 \\ 2 & 3 \end{bmatrix} \quad \text{change sign}$$

$$K^{-1} = \frac{1}{9} \begin{bmatrix} 5 & -3 \\ -2 & 3 \end{bmatrix}$$

$$= \frac{1}{9} \begin{bmatrix} 5 & -3 \\ -2 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 5(9^{-1}) & (-3)9^{-1} \\ (-2)9^{-1} & (3)9^{-1} \end{bmatrix}$$

we know $9^{-1} \text{ mod } 26 = 3$

$$\Rightarrow \begin{bmatrix} 5(3) & (-3)(3) \\ (-2)(3) & (3)(3) \end{bmatrix}$$

$$= \begin{bmatrix} 15 & -9 \\ -6 & 9 \end{bmatrix} \pmod{26}$$

$$= 3 \begin{bmatrix} 5 & -3 \\ -2 & 3 \end{bmatrix} \pmod{26}$$

$$= 3 \begin{bmatrix} 5 & 23 \\ 24 & 3 \end{bmatrix} \pmod{26}$$

$$= \begin{bmatrix} 15 & 69 \\ 72 & 9 \end{bmatrix} \pmod{26}$$

$$= \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix}$$

$$-9 \pmod{26}$$

$$\Rightarrow -9 + 26 = 17$$

$$-3 + 26 = 23$$

$$-2 + 26 = 24$$

additional step

$$\text{Hence } P = \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix} \begin{bmatrix} 7 \\ 8 \end{bmatrix} \pmod{26} \Rightarrow \begin{bmatrix} 105 & 136 \\ 140 & 72 \end{bmatrix}$$

$$= \begin{bmatrix} 241 \\ 212 \end{bmatrix} \pmod{26} = \begin{bmatrix} 7 \\ 4 \end{bmatrix} \Rightarrow \begin{bmatrix} H \\ E \end{bmatrix}$$

Similarly for AT

$$P = \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix} \begin{bmatrix} 0 \\ 19 \end{bmatrix} \pmod{26}$$

$$= \begin{bmatrix} 323 \\ 171 \end{bmatrix} \pmod{26}$$

$$= \begin{bmatrix} 11 \\ 15 \end{bmatrix} = \begin{bmatrix} L \\ P \end{bmatrix}$$

hence HELP.

H/W:

Playfair - keyword monarchy

P-T - Balloon

Caesar, cipher - P-T - meet me after the toga party

key = 3

Hill cipher: - "pay more money" - PT

$$\text{key} = \begin{bmatrix} 17 & 7 & 5 \\ 21 & 19 & 21 \\ 2 & 2 & 19 \end{bmatrix}$$

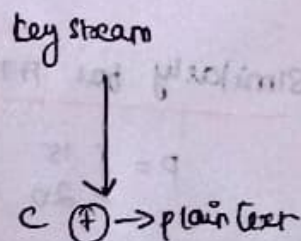
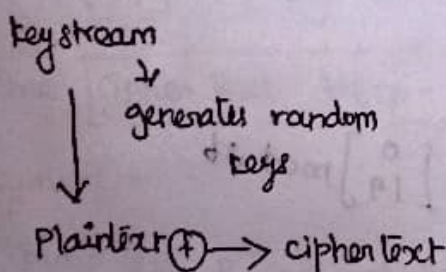
Ex: 2 PT. Hill cipher

$$\text{key} = \begin{pmatrix} 7 & 2 \\ 17 & 25 \end{pmatrix} \quad \text{HCRZSSXNSP}$$

VERNAM CIPHER

It is a poly alphabetic cipher.

- > main aim of cryptanalysis is to choose a keyword.
- > This was introduced by AT & T engineer Gilbert Vernam in 1918.
- > This works on binary data rather than letters.



$$C_i = P_i \oplus K_i$$

P_i - binary digit of plaintext

K_i - binary digit of key.

C_i - binary digit of cipher text.

Ex: Vernam cipher also called OTP (one time pad).

plain text: Hello

key - any random key where PT + key length should be same.

Key: NCBTA

Encryption:

P:	H	E	L	L	O
	7	4	11	11	14
K:	N	C	B	T	A
	13	2	1	19	0
<hr/>					
	20	6	12	30	14
				-26	
				4	
<hr/>					

There are only 26 alphabets. Hence we have to subtract 26 from 30

Cipher text: U G M E D

Decryption:- C-K

C:	U	G	M	E	O
	20	6	12	4	0
	20	6	12	30	0
K:	N	C	B	T	A
	13	2	1	19	0
<hr/>					
	7	4	11	11	14
<hr/>					

→ Add 26 to avoid negative result

P: H E L L O → hence plain text

Ans:
PT: WORLD
key: TEJAS.
find CT.

Adv:

- The key is used for encryption and decryption and then that key can be discarded.
- one time pad - is unbreakable.
- There is no statistical relationship b/w PT, hence, there is no simple way for breaking the code :-

Polyalphabetic cipher:

Another way for improving simple monoalphabetic technique called polyalphabetic cipher.

→ Vignere

↳ auto key system where key word is concatenated with plaintext to provide running key.

Ex:- attack at dawn

key: lemon.

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
A	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
B	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A
C	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B
D	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C
E	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D
F	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E
G	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F
H	H	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G
I	I	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H
J	J	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I
K	K	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J
L	L	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K
M	M	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L
N	N	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M
O	O	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	P	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	Q	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	R	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	S	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	T	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S

attack at dawn
 lemonlemonle

ciphertext: - LXFOPVEFRNHR

lemonlemonle

attack
 hav

attack at dawn.

Method II:

using key table.

key: deceptive deceptive -> has to repeat the keyword.

PT: we are discovered by save yourself.

CT: ZICVTWQNHURZGVTWAVZHCRQYGLMGJ

key	3	4	2	4	15	19	8	21	4	3	4	2	4	15	19
PT	22	4	0	17	4	3	8	18	2	14	21	4	17	4	3
CT	25	8	2	21	19	22	16	13	6	17	25	6	21	19	22

have to
 add key and PT

key	8	21	4	3	4	2	4	15	19	8	21	4
PT	18	0	21	4	24	14	20	17	18	4	11	5
CT	26	21	25	7	2	18	24	26	16	12	6	9

CRYPTANALYSIS:

This vigenere cipher is unbreakable, due to the use of 26 different cipher alphabets.

Disadvantage:

-> If the key length is smaller than plaintext length, then key will be repeated. . . due to repeating nature of key.

-> This is computationally secured.