



TOPIC : 8 – Tutorial 2

- 1. Show that $R \lor S$ follows logically from the premises $C \lor D$, $(C \lor D) \rightarrow \exists H, \exists H \rightarrow (A \land \exists B)$ and $(A \land \exists B) \rightarrow (R \lor S)$.
- **2.** Show that $(P \rightarrow Q) \land (R \rightarrow S)$, $(Q \land M) \land (S \rightarrow N)$, $\exists (M \land N) \text{ and } (P \rightarrow R) \Rightarrow \exists P$
- 3. Show that $R \land (P \lor Q)$ is a valid conclusion from the premises $P \lor Q$, $Q \rightarrow R$, $P \rightarrow M$, $\forall M$.
- **4.** Prove that the premises $a \rightarrow (b \rightarrow c)$, $d \rightarrow (b \land \neg c)$ and $(a \land d)$ are inconsistent.
- **5.** Prove that the premises $P \rightarrow Q$, $Q \rightarrow R$, $R \rightarrow S$, $S \rightarrow \exists R$, $P \land S$ are inconsistent.
- 6. Show that $R \rightarrow S$ can be derived from the premises $P \rightarrow (Q \rightarrow S)$, $\exists R \lor P \& Q$
- 7. Using conditional proof prove that $P \lor Q$, $Q \lor R$, $R \rightarrow S \Rightarrow P \rightarrow S$
- 8. Prove that $A \rightarrow \neg D$ is a conclusion from the premises $A \rightarrow B \lor C$, $B \rightarrow \neg A$ and $D \rightarrow \neg C$ by using conditional proof.
- 9. Show that the following set of premises are inconsistent
 - (i) If Jack misses many classes through illness, then he fails high school
 - (ii) If Jack fails high school, then he is uneducated
 - (iii) If Jack reads a lot of books, then he is not uneducated.
 - (iv) Jack misses many classes through illness and reads a lot of books.
- 10. Show that the premises "One student in this class knows how to write a program in JAVA", and Everyone who knows how to write a program in JAVA can get a high paying job imply a conclusion " someone in the class can get high paying job.