



TUTORIAL-1

Problems based on Fourier Integral and Fourier Transform.

1. Find the Fourier integral of the function $f(x) = \begin{cases} 0, & x < 0 \\ 1/2, & x = 0 \\ e^{-x}, & x > 0 \end{cases}$

2. Find the Fourier transform of $f(x) = \begin{cases} \sin x, & x < 0 < \pi \\ 0, & \pi < 0 < \infty \end{cases}$

3. Find the Fourier transform of the function $f(x)$ defined by $f(x) = \begin{cases} 1 - x^2 & \text{if } |x| < 1 \\ 0 & \text{if } |x| \geq 1 \end{cases}$.

Hence, prove that $\int_0^{\infty} \frac{\sin s - s \cos s}{s^3} \cos\left(\frac{s}{2}\right) ds = \frac{3\pi}{16}$

also show that $\int_0^{\infty} \left(\frac{\sin t - t \cos t}{t^3} \right)^2 dt = \frac{\pi}{15}$