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Topic: 1.3 - PROBLEMS ON EIGEN VALUES AND EIGEN VECTORS

Find the Eigen value and Eigen Vectors of (2 1-6) 80lu: Het $A = \begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \end{pmatrix}$ step:1: to find the char. egr. The chairegu. Of A is $\lambda^3 - S_1 \lambda^2 + S_2 \lambda - S_3 = 0$ where S. = Sum of the main diagonali elements = -2+1+0 82 - 8um of the minors of the main diagonal elements. $= \begin{vmatrix} 1 & -b \\ -2 & 0 \end{vmatrix} + \begin{vmatrix} -2 & -3 \\ -1 & 0 \end{vmatrix} + \begin{vmatrix} -2 & 2 \\ 2 & 1 \end{vmatrix}$ = (0-12)+ (0-3)+ (-2-4) = -12-3-6 =-21 8 = 1A1 - -2(0-12)-2(0-6)-3(-4+1) = 24+12+9=45 e Char. Pgu. 15 23 + 2-21 2-45 = 0





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8 tep 2: to solve the char. equ.
$$0.3+0.2-210-45=0$$
 — 0.0
The D=1 there=1+1-21-45 ± 0.0
The D=1 there=1+1-21-45 ± 0.0

54
$$\lambda = 2$$
, $0 \Rightarrow 8 + 4 - 42 - 45 \pm 0$

53 $\lambda = -2$, $0 \Rightarrow -8 + 4 + 42 - 45 \pm 0$

54 $\lambda = 3$, $0 \Rightarrow 24 + 9 - 63 - 45 \pm 0$

54 $\lambda = -3$, $0 \Rightarrow -24 + 9 + 63 + 45 = 0$

14 $\lambda = -3$, $0 \Rightarrow -24 + 9 + 63 + 45 = 0$

14 $\lambda = -3$ is a root of $\lambda^3 + \lambda^2 - 21\lambda - 45 = 0$.

15 $\lambda^3 + \lambda^2 - 21\lambda - 45 = (\lambda + 3) (\lambda^3 - 2\lambda - 15) = 0$

16 (ie) $(\lambda + 3)$ $(\lambda + 3)$ $(\lambda - 5) = 0$

17 $\lambda = -3$, $\lambda = 3$, $\lambda = 5$

8 Eep: 3 to find the Figenvectors.

Solve
$$(A-\lambda i) \times = 0$$

$$\begin{bmatrix} -2-\lambda & 2 & -3 \\ 2 & 1-\lambda & -6 \\ -1 & -2 & 0-\lambda \end{bmatrix} \begin{bmatrix} \chi_1 \\ \chi_2 \\ \chi_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$





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Case(i):
$$54 \ N = -3 \ \text{then} \ \text{eqs. (A)} \ \text{becomes} \ .$$

$$\begin{pmatrix} 1 & 2 & -3 \\ 2 & 3 & -6 \\ -1 & -2 & 3 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ 3_3 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

$$x_1 + 2x_2 - 3x_3 = 0 \qquad \text{(B)}$$

$$2x_1 + 4x_2 - 6x_3 = 0 \qquad \text{(B)}$$

$$-x_1 - 2x_2 + 3x_3 = 0 \qquad \text{(F)}$$
Here 0 , 0 be 0 are some equ.

We consider
$$x_1+2y_2-3x_3=0$$

Put $x_1=0$ We get $2x_2=3x_3$

$$\frac{x_2}{3}=\frac{x_3}{3}$$

$$\frac{x_3}{3}=\frac{x_3}{3}$$

Put $x_2=0$, We get $x_1-3x_3=0$

$$x_1=3x_3=0$$

$$x_1=3x_1=0$$

$$x_1=3$$





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5d
$$N = 5$$
 then $Q\mu$. (a) becomes.

$$\begin{pmatrix}
-7 & 2 & -3 \\
2 & -4 & -6
\\
-1 & -2 & -5
\end{pmatrix}
\begin{pmatrix}
x_1 \\
x_2 \\
x_3
\end{pmatrix} = \begin{pmatrix}
0 \\
0 \\
0
\end{pmatrix}$$

$$-741 + 24 - 343 = 0$$

$$-741 - 44 - 543 = 0$$

$$-741 - 24 - 543 = 0$$
Solving (a) 60 We get
$$-741 - 7$$





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Find the Figenvalues and Eigenvectors

$$\begin{pmatrix}
6 & -b & 5 \\
14 & -13 & 10 \\
7 & -b & A
\end{pmatrix}$$
80lu: Let $A = \begin{pmatrix}
b & -b & 5 \\
14 & -13 & 10 \\
7 & -b & A
\end{pmatrix}$

Step1: to find the Chan equ.
The Chan: equ. of A is $A^3 - S, \lambda^2 + S_3 \lambda - S_3 = 0$ S1 = 6-13+4 = -3

$$S_{2} = \begin{vmatrix} -13 & 10 \\ -6 & 4 \end{vmatrix} + \begin{vmatrix} 6 & 5 \\ 7 & 4 \end{vmatrix} + \begin{vmatrix} 6 & -6 \\ 14 & -13 \end{vmatrix}$$

$$= (-52 + 60) + (24 - 35) + (-78 + 84)$$

$$= 8 - 14 + 6 = 3$$

$$S_3 = |A| = -1$$





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$$(\lambda+1) \ (\lambda^{2}+2\lambda+1) = 0$$

$$(\lambda+1) \ (\lambda+1) \ (\lambda+1) \ (\lambda+1) = 0$$
Hence the Eigenvalues are -1,-1,-1

Step: 3 To find the Eigenvector,

$$801 \text{ ve } (A-\lambda 1) \times = 0$$

$$(b-\lambda - b + 5) \times (x_{1}) = 0$$

$$(b-\lambda - b + 5) \times (x_{2}) = 0$$
When $\lambda = -1$, A becomes.
$$(\lambda+1) \ (\lambda+1) \times (\lambda+1) = 0$$

$$(\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) = 0$$

$$(\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) = 0$$

$$(\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) = 0$$

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$$(\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) \times (\lambda+1) = 0$$

$$(\lambda+1) \times (\lambda+1) \times (\lambda+1)$$





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Find the Eigenvalues and Eigenvector of (100) Let A = (0 1 1 1) 8 tep: 1: To find the characteristic equ. The Chan: egu. of A 15 13-5, 12,52-53=0 Where S1 = 0+0+0 = 0 S== 10 1)+ 10 1)+ 10 1) = (0-17+ (0-17+ (0-17) S3 = 1A1 = 0 (0-1)-1 (0-1)+1(1-0) = 0+1+1=2 ... The char. equ. 15 $\lambda^3 - 0\lambda^2 - 3\lambda - 2 = 0$ 3 tep: 2: To find Eigen Value. Solvier 23_37-2=0 St 7=1, 0 =) 1-3-2 = 0 If $\lambda = -1$, 0 = -1+3-2 = 0(ie) (x=)-2)=0





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Hence the Eigenvalues are
$$-1,-1,2$$
.

Step:3 to find Eigenvalues are $-1,-1,2$.

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Solve $(A-N)X = 0$ (ie) $\frac{1}{1} - \frac{1}{2} = \frac{1}$





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Here
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Put $\chi_1 = 0$ We get $\chi_2 = -\chi_3$
 $\chi_2 = \chi_3$
 $\chi_3 = \chi_3$
 $\chi_4 = \chi_5$

Ergen Vedox $\chi_4 = \{0\}$