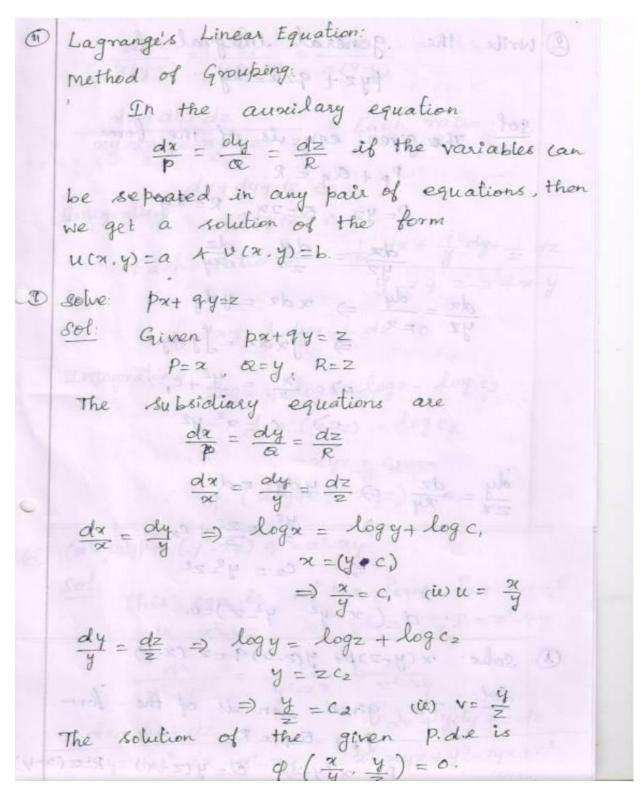




#### **TOPIC: 7 - LAGRANGE'S EQUATION - METHOD OF GROUPING**







@ write the general integral of gol: The given eqn is of the form P = yz, 0 = 2x, R = xydx = dy = dz xy sa (y. R) W  $\frac{d\alpha}{yz} = \frac{dy}{z^2} \Rightarrow x dz = y dy$   $\Rightarrow \int x dx = \int y dy$  $\frac{x^2}{2} = \frac{y^2}{2} + c$ dz = ydy=zdz =  $\frac{y^2}{3} = \frac{22}{3} + c_2$ · q (x2-y2, y2-22)=0. Solve: x (y-2)p+ y(z-x) 9= z (x-4) 3 Sol The given egn is of the form at also apply digit Rio middles is D= x (4-2) Q= y(z-x) R=z(x-4)





$$\frac{dx}{x_1y_2} = \frac{dy}{y(z_-x)} = \frac{dz}{z(2-y)}$$

$$\frac{dx + dy + dz}{xy_-xz_+yz_-xy} = \frac{z}{z_-x_-zy}$$

$$\frac{dx + dy + dz}{z_-zy} = \frac{z}{z_-x_-zy}$$

$$\frac{dx + dy + dz}{z_-zy} = \frac{1}{z_-x_-} \frac{dx + \frac{1}{y}}{z_-x_-} \frac{dy + \frac{1}{z}}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{1}{z_-x_-} \frac{dx + \frac{1}{y}}{z_-z_-} \frac{dy + \frac{1}{z}}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{1}{z_-x_-} \frac{dx + \frac{1}{y}}{z_-z_-} \frac{dy + \frac{1}{z}}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{1}{z_-z_-} \frac{dx + \frac{1}{y}}{z_-z_-} \frac{dy}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{1}{z_-z_-} \frac{dx + \frac{1}{z_-}}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{1}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{dx + dy + dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{dx + dy + dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-}$$

$$\frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{dz}{z_-z_-} \frac{z_-z_-}{z_-z_-} \frac{dz}{z_-}$$





$$\frac{x \, dx + y \, dy + z \, dz}{x^3 + y^3 + z^3 - 3xyz} = \frac{dx + dy + dz}{x^2 + y^2 + z^2 - xy - yz - zx}$$

$$\frac{x \, dx + y \, dy + z \, dz}{(x + y + z) (x^2 + y^2 + z^2 - xy - yz + zx)} = \frac{dx + dy + dz}{x^2 + y^2 + z^2 - xy - yz + zx}$$

$$\frac{x \, dx + y \, dy + z \, dz}{-yz + zx} = (x + y + z) (dx + dy + dz)$$
This grating,
$$\frac{x^2}{2} + \frac{y^2}{2} + \frac{z^2}{2} = \frac{(x + y + z)^2}{2} + C$$

$$\frac{x^2 + y^2 + z^2}{2} = (x + y + z)^2 + C$$

$$\frac{x^2 + y^2 + z^2}{2} = (x + y + z)^2 + C$$

$$\frac{x^2 + y^2 + z^2}{2} = x^2 + y^2 + z^2 + 2xy + 2yz + 2zx + C$$

$$-2(xy + yz + zx) = C$$

$$xy + yz + zx = u \quad Cuontant)$$

$$\frac{dx - dy}{x^2 - y^2 - y^2 + zx} = \frac{dy - dz}{y^2 - zx - z^2 + xy}$$

$$\frac{d(x - y)}{(x^2 + y^2 + z^2)} = \frac{d(y - z)}{(y - z)(y + z^2 + z)}$$

$$\frac{d(x - y)}{(x + y + z^2)} = \frac{d(y - z)}{(y - z)(y + z^2 + z)}$$





Integrating on both sides, we get  $\log (x-y) = \log (y-2) + \log c$   $\log (x-y) - \log (y-2) = \log c$   $\log \frac{x-y}{y-2} = \log c$   $\frac{x-y}{y-2} = c$ The general solution is  $\varphi \left(xy+yz+2x, \frac{x-y}{y-z}\right) = 0.$