



Structure of the Page Table



- Memory structures for paging can get huge using straight-forward methods
 - Consider a 32-bit logical address space as on modern computers
 - Page size of 4 KB (2^{12})
 - Page table would have 1 million entries ($2^{32} / 2^{12}$)
 - If each entry is 4 bytes -> 4 MB of physical address space / memory for page table alone
 - That amount of memory used to cost a lot
 - Don' t want to allocate that contiguously in main memory
- Hierarchical Paging
- Hashed Page Tables
- Inverted Page Tables



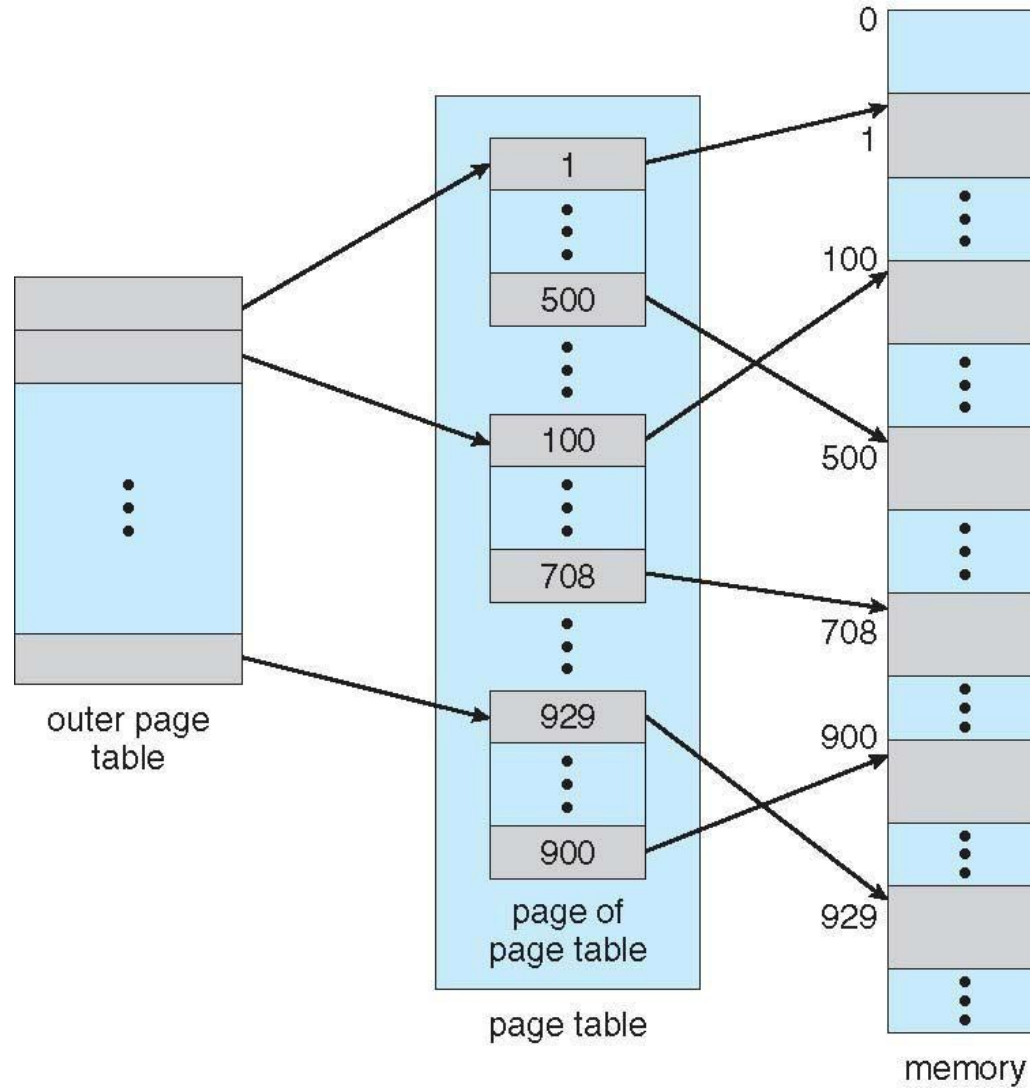
Hierarchical Page Tables



- Break up the logical address space into multiple page tables
- A simple technique is a two-level page table
- We then page the page table



Two-Level Page-Table Scheme





Two-Level Paging Example

- A logical address (on 32-bit machine with 1K page size) is divided into:
 - a page number consisting of 22 bits
 - a page offset consisting of 10 bits
- Since the page table is paged, the page number is further divided into:
 - a 12-bit page number
 - a 10-bit page offset

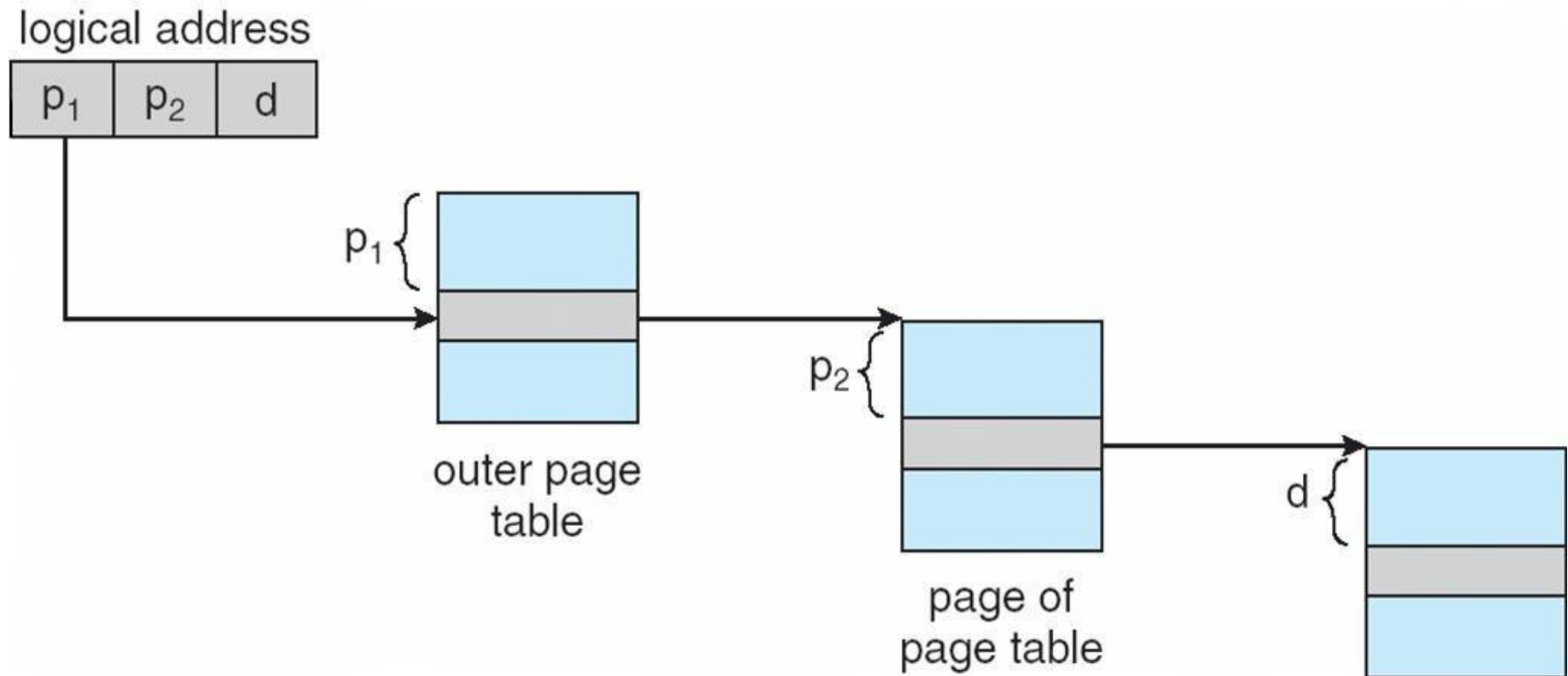
- Thus, a logical address is as follows:

page number		page offset
p_1	p_2	d
12	10	10

- where p_1 is an index into the outer page table, and p_2 is the displacement
- within the page of the inner page table Known as **forward-mapped page table**



Address-Translation Scheme





64-bit Logical Address Space

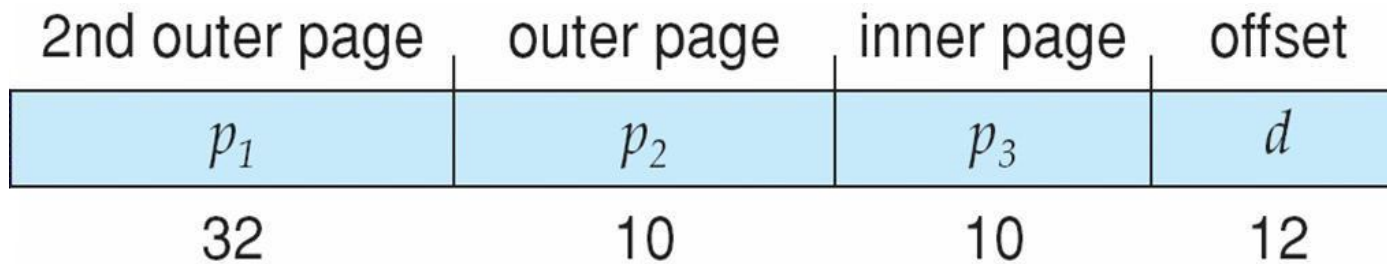
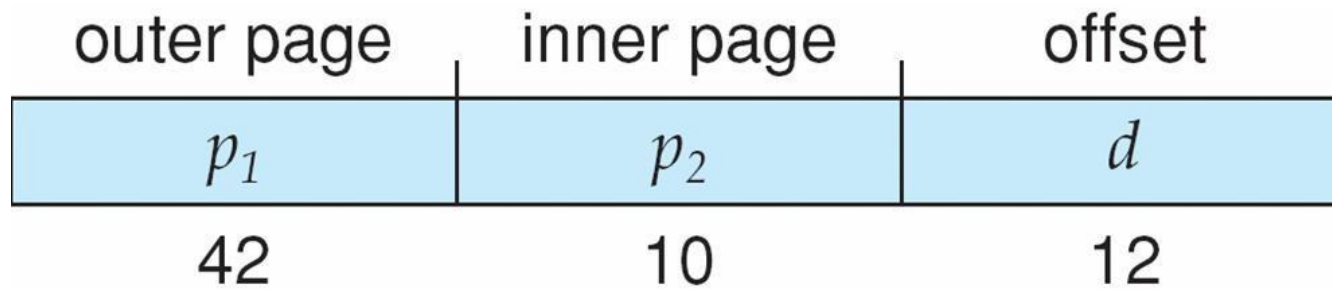
- Even two-level paging scheme not sufficient
- If page size is 4 KB (2^{12})
 - Then page table has 2^{52} entries
 - If two level scheme, inner page tables could be 2^{10} 4-byte entries
 - Address would look like

outer page	inner page	page offset
p_1	p_2	d
42	10	12

- Outer page table has 2^{42} entries or 2^{44} bytes
- One solution is to add a 2nd outer page table
- But in the following example the 2nd outer page table is still 2^{34} bytes in size
 - And possibly 4 memory access to get to one physical memory location



Three-level Paging Scheme





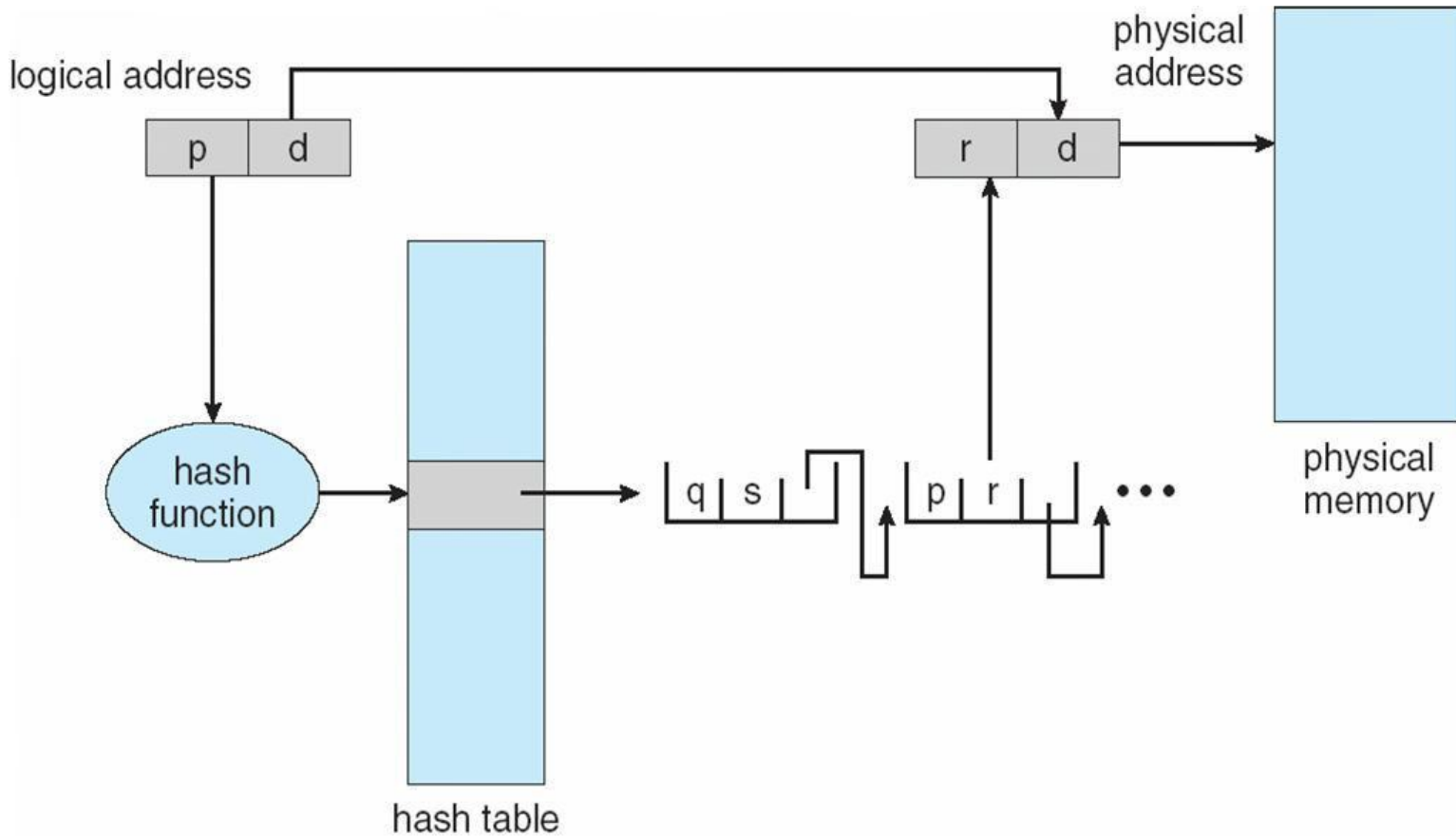
Hashed Page Tables



- Common in address spaces > 32 bits
- The virtual page number is hashed into a page table
 - This page table contains a chain of elements hashing to the same location
- Each element contains (1) the virtual page number (2) the value of the mapped page frame (3) a pointer to the next element
- Virtual page numbers are compared in this chain searching for a match
 - If a match is found, the corresponding physical frame is extracted
- Variation for 64-bit addresses is **clustered page tables**
 - Similar to hashed but each entry refers to several pages (such as 16) rather than 1
 - Especially useful for **sparse** address spaces (where memory references are non-contiguous and scattered)



Hashed Page Table



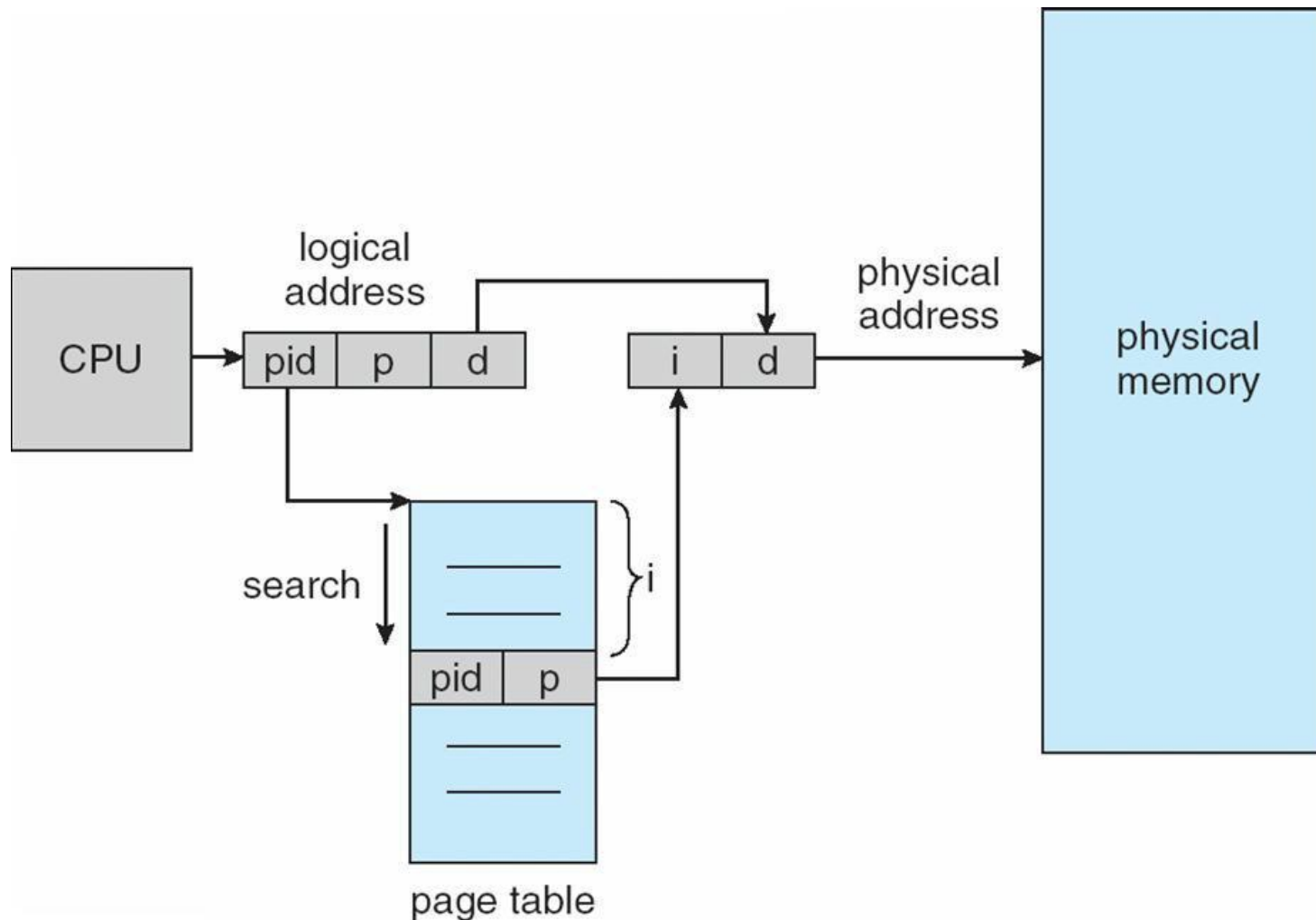


Inverted Page Table

- Rather than each process having a page table and keeping track of all possible logical pages, track all physical pages
- One entry for each real page of memory
- Entry consists of the virtual address of the page stored in that real memory location, with information about the process that owns that page
- Decreases memory needed to store each page table, but increases time needed to search the table when a page reference occurs
- Use hash table to limit the search to one — or at most a few — page-table entries
 - TLB can accelerate access
- But how to implement shared memory?
 - One mapping of a virtual address to the shared physical address



Inverted Page Table Architecture





Oracle SPARC Solaris



- Consider modern, 64-bit operating system example with tightly integrated HW
 - Goals are efficiency, low overhead
- Based on hashing, but more complex
- Two hash tables
 - One kernel and one for all user processes
 - Each maps memory addresses from virtual to physical memory
 - Each entry represents a contiguous area of mapped virtual memory,
 - More efficient than having a separate hash-table entry for each page
 - Each entry has base address and span (indicating the number of pages the entry represents)



Oracle SPARC Solaris (Cont.)



- TLB holds translation table entries (TTEs) for fast hardware lookups
 - A cache of TTEs reside in a translation storage buffer (TSB)
 - Includes an entry per recently accessed page
- Virtual address reference causes TLB search
 - If miss, hardware walks the in-memory TSB looking for the TTE corresponding to the address
 - If match found, the CPU copies the TSB entry into the TLB and translation completes
 - If no match found, kernel interrupted to search the hash table
 - The kernel then creates a TTE from the appropriate hash table and stores it in the TSB, Interrupt handler returns control to the MMU, which completes the address translation.



Example: The Intel 32 and 64-bit Architectures



- Dominant industry chips
- Pentium CPUs are 32-bit and called IA-32 architecture
- Current Intel CPUs are 64-bit and called IA-64 architecture
- Many variations in the chips, cover the main ideas here



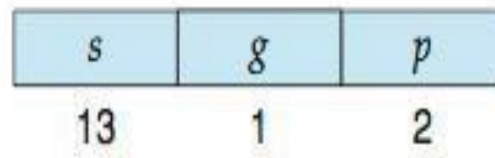
Example: The Intel IA-32 Architecture

- Supports both segmentation and segmentation with paging
 - Each segment can be 4 GB
 - Up to 16 K segments per process
 - Divided into two partitions
 - First partition of up to 8 K segments are private to process (kept in **local descriptor table (LDT)**)
 - Second partition of up to 8K segments shared among all processes (kept in **global descriptor table (GDT)**)



Example: The Intel IA-32 Architecture (Cont.)

- CPU generates logical address
 - Selector given to segmentation unit
 - Which produces linear addresses

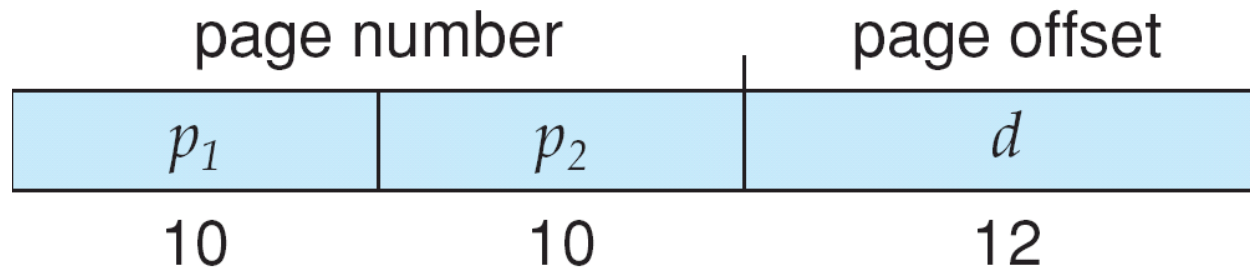
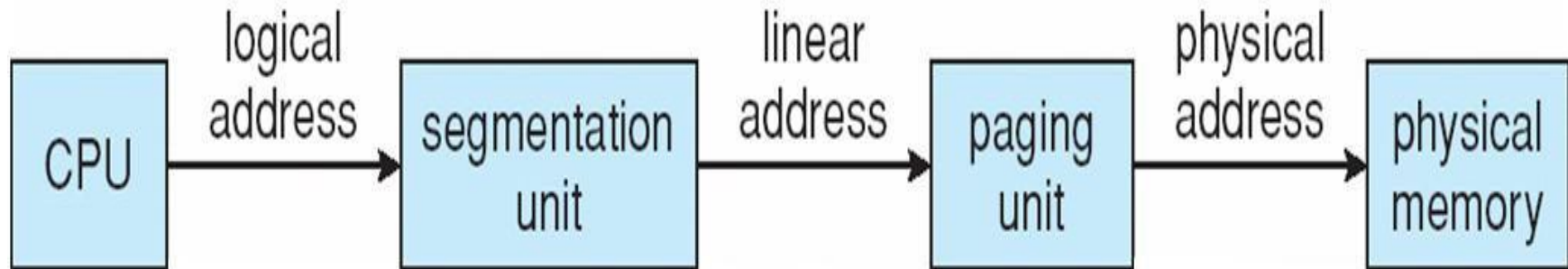


- Linear address given to paging unit
 - Which generates physical address in main memory
 - Paging units form equivalent of MMU
 - Pages sizes can be 4 KB or 4 MB



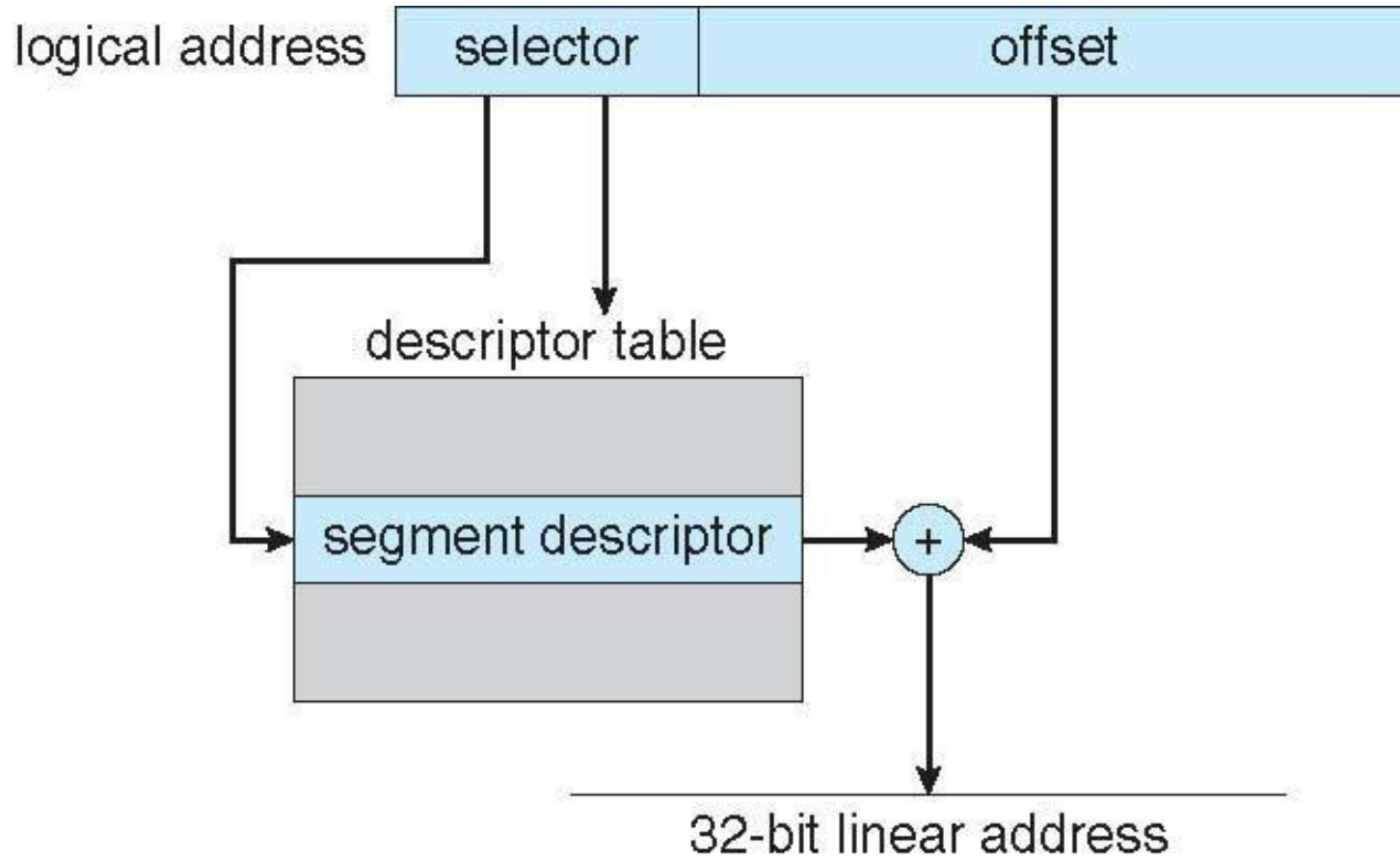
Logical to Physical Address

Translation in IA-32



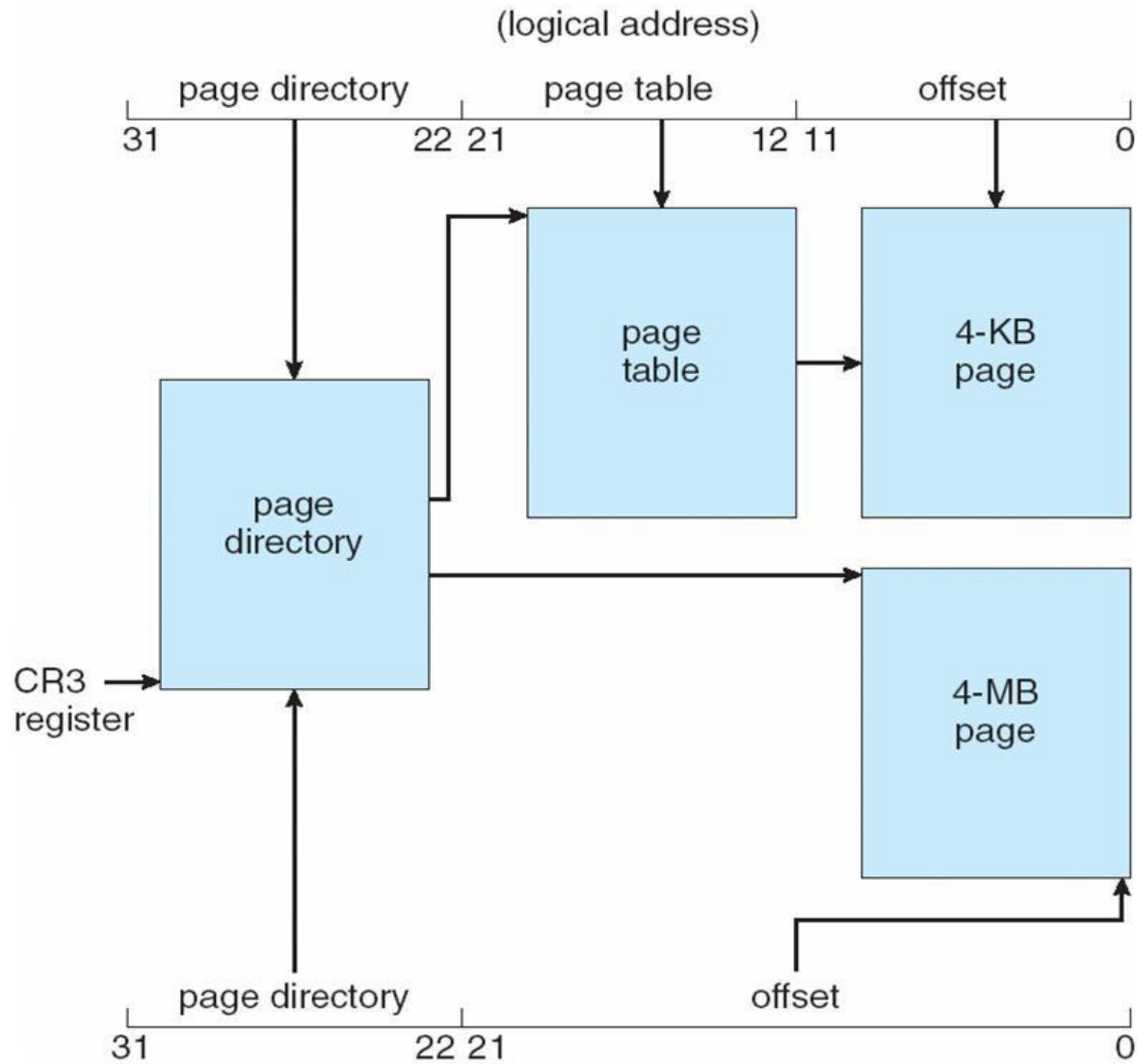


Intel IA-32 Segmentation





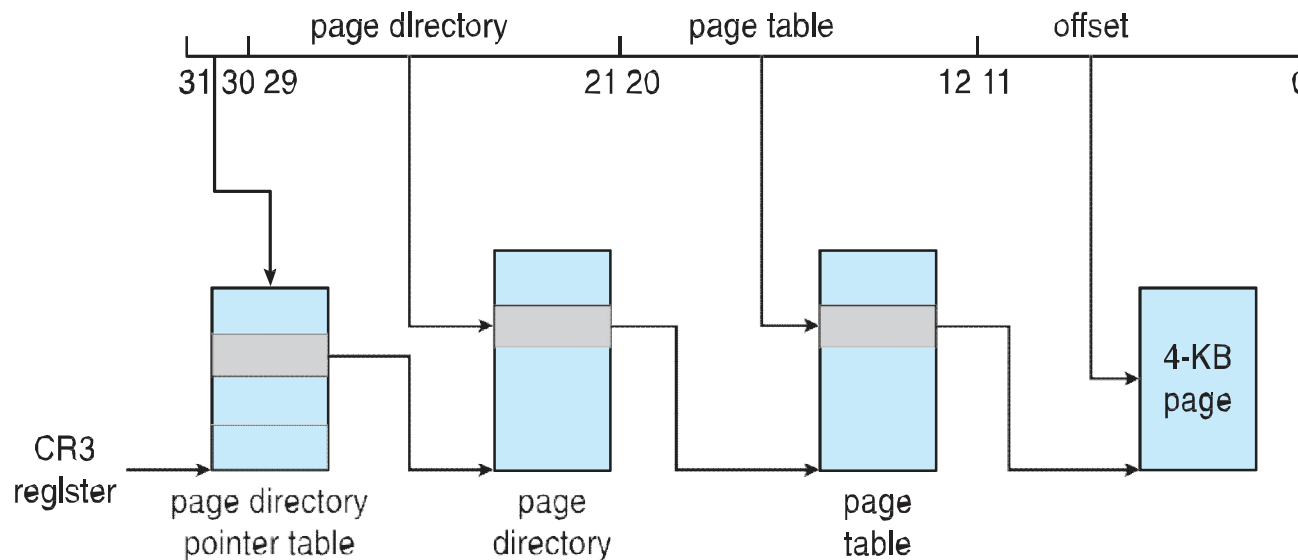
Intel IA-32 Paging Architecture





Intel IA-32 Page Address Extensions

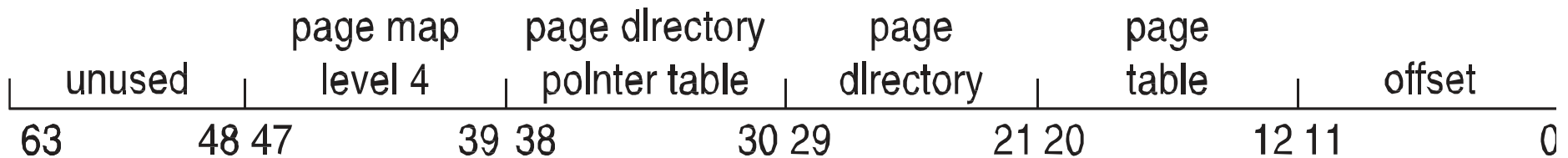
- 32-bit address limits led Intel to create **page address extension (PAE)**, allowing 32-bit apps access to more than 4GB of memory space
 - Paging went to a 3-level scheme
 - Top two bits refer to a **page directory pointer table**
 - Page-directory and page-table entries moved to 64-bits in size
 - Net effect is increasing address space to 36 bits – 64GB of physical memory





Intel x86-64

- Current generation Intel x86 architecture
- 64 bits is ginormous (> 16 exabytes)
- In practice only implement 48 bit addressing
 - Page sizes of 4 KB, 2 MB, 1 GB
 - Four levels of paging hierarchy
- Can also use PAE so virtual addresses are 48 bits and physical addresses are 52 bits





Example: ARM Architecture

- Dominant mobile platform chip
(Apple iOS and Google Android devices for example)
- Modern, energy efficient, 32-bit CPU
- 4 KB and 16 KB pages
- 1 MB and 16 MB pages (termed **sections**)
- One-level paging for sections, two-level for smaller pages
- Two levels of TLBs
 - Outer level has two micro TLBs (one data, one instruction)
 - Inner is single main TLB
 - First inner is checked, on miss outers are checked, and on miss page table walk performed by CPU

