

SWITCHED RELUCTANCE MOTOR

Basic voltage equation of SRM is given by

$$V = Ri + \frac{d\lambda}{dt} [\lambda = Li]$$

where,

$V \rightarrow$ input Voltage

$i \rightarrow$ current through phase winding

$R \rightarrow$ resistance of phase winding

$\lambda \rightarrow$ flux linkage = Li

$$\frac{d\lambda}{dt} = \frac{d(Li)}{dt}$$

$$\frac{\partial \lambda}{\partial t} = \frac{\partial i}{\partial t} (L) + \frac{\partial L}{\partial t} (i)$$

$$= L \frac{\partial i}{\partial t} + i \frac{\partial L}{\partial \theta} \cdot \frac{d\theta}{dt}$$

$$= L \frac{\partial i}{\partial t} + i \omega \frac{\partial L}{\partial \theta} \quad \text{where } \omega = \frac{\partial \theta}{\partial t}$$

$$V = iR + L \frac{\partial i}{\partial t} + i \omega \frac{\partial L}{\partial \theta} \quad \text{--- (1)}$$

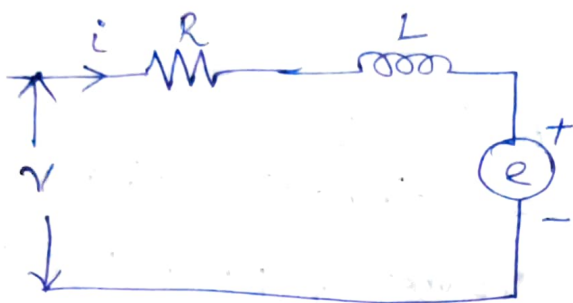
$$V = iR + L \frac{\partial i}{\partial t} + e \quad \text{--- (2)}$$

It is the voltage eq. of SRM.

where $R \rightarrow$ resistive drop

$L \frac{di}{dt} \rightarrow$ emf due to inductance

$i\omega \frac{\partial L}{\partial \theta} = e \rightarrow$ self emf.



eq. circuit

Multiply i on both sides in eq. (1)

$$V_i = \left(Ri + L \frac{di}{dt} + i\omega \frac{\partial L}{\partial \theta} \right) i$$

$$= i^2 R + Li \frac{di}{dt} + i^2 \omega \frac{\partial L}{\partial \theta} \quad \text{--- (3)}$$

where,

$V_i =$ electrical power supplied (w)

$i^2 R =$ resistive losses.

$Li \frac{di}{dt} =$ power associated with incremental inductance

$i^2 \omega \frac{\partial L}{\partial \theta} = ei \rightarrow$ power due to self emf

stored energy in magnetic

$$\text{field} = \frac{1}{2} Li^2$$

power associated with

$$\text{change in stored energy} = \frac{dW_{st}}{dt}$$

$$\frac{dW_{st}}{dt} = \frac{1}{2} L (2i) \frac{di}{dt} + \frac{1}{2} i^2 \frac{dL}{dt}$$

$$= Li \frac{di}{dt} + \frac{1}{2} i^2 \frac{dL}{d\theta} \cdot \frac{d\theta}{dt}$$

$$= Li \frac{di}{dt} + \frac{1}{2} i^2 \omega \frac{dL}{d\theta} \quad \text{--- (4)}$$

$P_m = Vi - i^2 R$ - power associated with change in stored energy

$$= Vi - i^2 R - \frac{dW_{st}}{dt} \quad \text{--- (5)}$$

Sub eq (3), (4) & (5)

$$P_m = \frac{1}{2} i^2 \omega \frac{dL}{d\theta} \quad \text{--- (6)}$$

Torque developed by arm

$$T = P_m / \omega$$

$$T = \frac{1}{2} i^2 \frac{dL}{d\theta} \quad \text{N-m}$$