



DIGITAL ELECTRONICS:
K-MAP



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DEPARTMENT OF ELECTRICAL AND ELECTRONICS ENGINEERING

INTRODUCTION TO K-MAP

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K-MAP

The complexity of the digital logic gates that implement a Boolean function is directly related to the complexity of the algebraic expression from which the function is implemented.

A map method provides a simple, straight forward procedure for minimizing Boolean functions.

This method may be regarded as a pictorial form of a truth table. The map method is also known as the **Karnaugh map or K-map.**



K-MAP



K-map can take two forms:

Sum of product (SOP)

Product of Sum (POS)



Steps to Solve Expression using K-map

- Select the K-map according to the number of variables.
- Identify minterms or maxterms as given in the problem.
- For SOP put 1's in blocks of K-map respective to the minterms (0's elsewhere).
- For POS put 0's in blocks of K-map respective to the max terms (1's elsewhere).
- Make rectangular groups containing total terms in power of two like 2,4,8 (except 1) and try to cover as many elements as you can in one group.
- From the groups made in step 5 find the product terms and sum them up for SOP form.

1. K-map of 3 variables

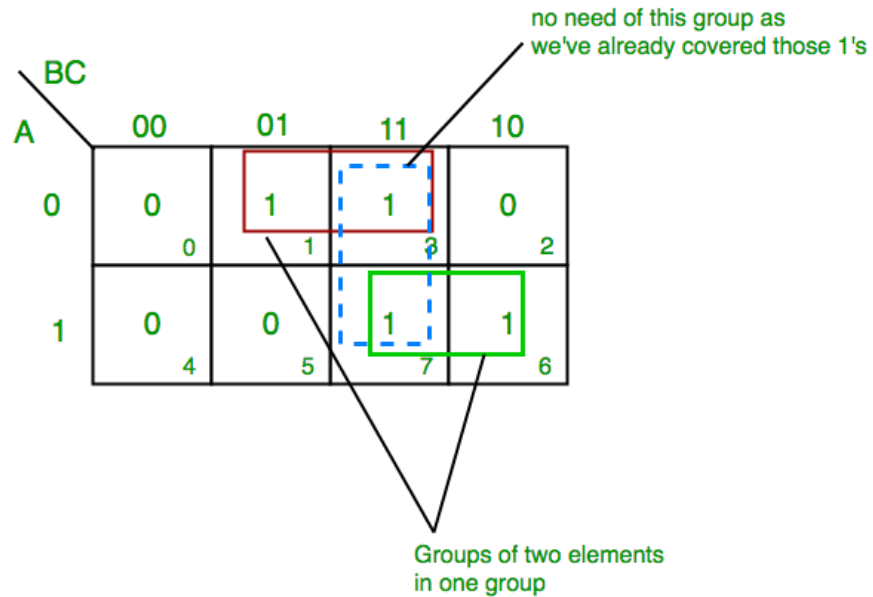
		BC			
		B'C'	B'C	BC	BC'
A	0	00	01	11	10
A'	0	A'B'C'	A'B'C	A'BC	A'BC'
		0	1	3	2
A	1	AB'C'	AB'C	ABC	ABC'
		4	5	7	6

SOP(MINTERMS)

- 8 Blocks = 1
- 4 Blocks = 1 variable term
- 2 Blocks = 2 variable term
- 1 Block = 3 variable term

K-map of 3 variables

$$F(A,B,C)=\Sigma(1,3,6,7)$$



From **red group** we get product term— $A'C$
 From **green group** we get product term— AB

Summing these product terms we get- Final expression $(A'C+AB)$

$$F= A'C+AB$$

K-map for 4 variables

		CD	C'D'	C'D	CD	CD'
		00	01	11	10	
A'B'	00	A'B'C'D'	A'B'C'D	A'B'CD	A'B'CD'	
		0	1	3	2	
A'B	01	A'BC'D'	A'BC'D	A'BCD	A'BCD'	
		4	5	7	6	
AB	11	ABC'D'	ABC'D	ABCD	ABCD'	
		12	13	15	14	
AB'	10	AB'C'D'	AB'C'D	AB'CD	AB'CD'	
		8	9	11	10	

SOP(MINTERMS)

16 Blocks = 1

8 Blocks = 1 variable term

4 Blocks = 2 variable term

2 Blocks = 3 variable term

1 Block = 4 variable term

K-map of 4 variables

$$F(A, B, C, D) = \Sigma m(0, 1, 2, 5, 7, 8, 9, 10, 13, 15)$$

		CD			
		$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
AB	$\bar{A}\bar{B}$	1 0	1 1	3	2 1
	$\bar{A}B$	4	1 5	1 7	6
	AB	12	1 13	1 15	14
	$A\bar{B}$	1 8	1 9	11	1 10

$$\begin{aligned}
 F(A, B, C, D) &= (A'B + AB)(C'D + CD) + (A'B' + A'B + AB + AB')C'D \\
 &+ (A'B' + AB')(C'D' + CD') \\
 &= BD + C'D + B'D'
 \end{aligned}$$

Thus, minimized boolean expression is-

$$F(A, B, C, D) = BD + C'D + B'D'$$

K-map of 4 variables

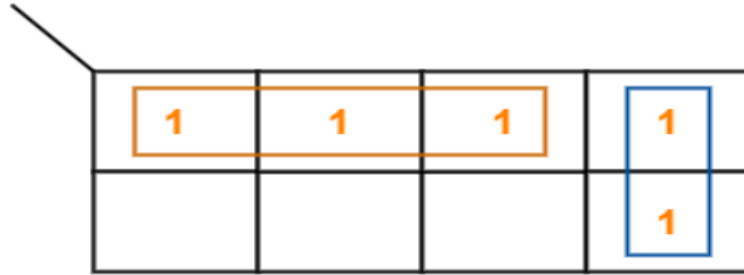
$$F(A, B, C, D) = \sum m(0, 1, 3, 5, 7, 8, 9, 11, 13, 15)$$

		CD			
		$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
AB	$\bar{A}\bar{B}$	1 0	1 1	1 3	2
	$\bar{A}B$	4	1 5	1 7	6
	AB	12	1 13	1 15	14
	$A\bar{B}$	1 8	1 9	1 11	10

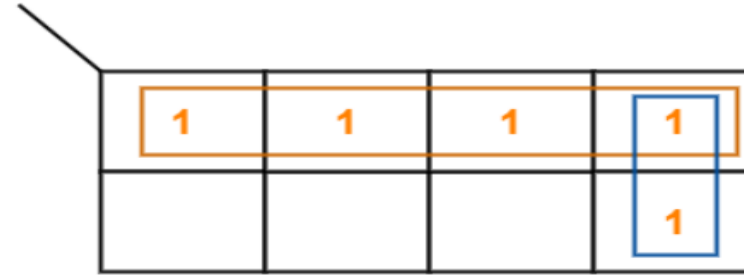
Minimized boolean expression is:

$$F(A, B, C, D) = B'C' + D$$

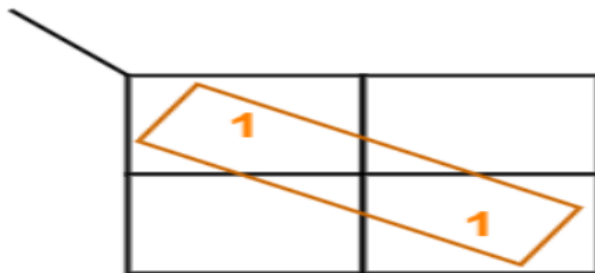
WRONG PRACTICES IN GROUPING



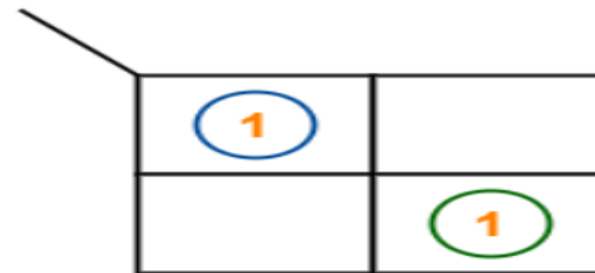
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Correct



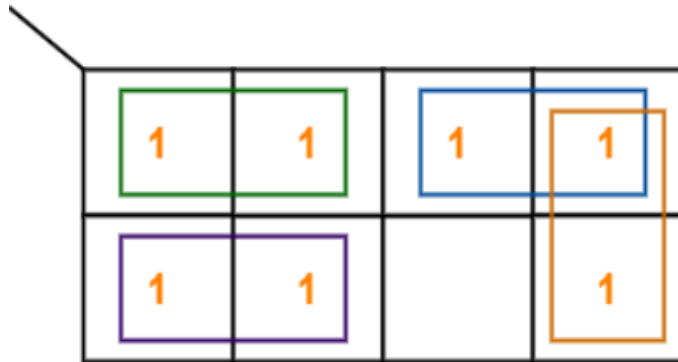
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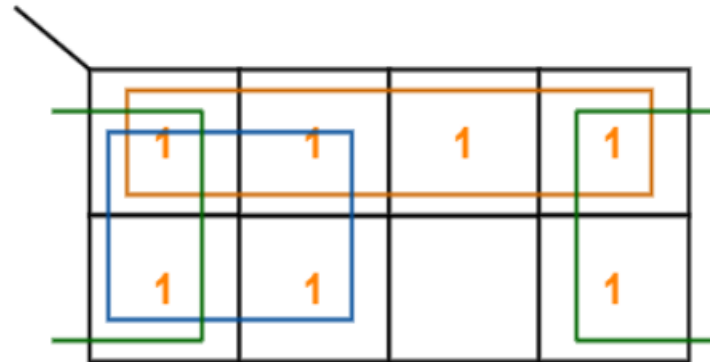
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WRONG PRACTICES IN GROUPING



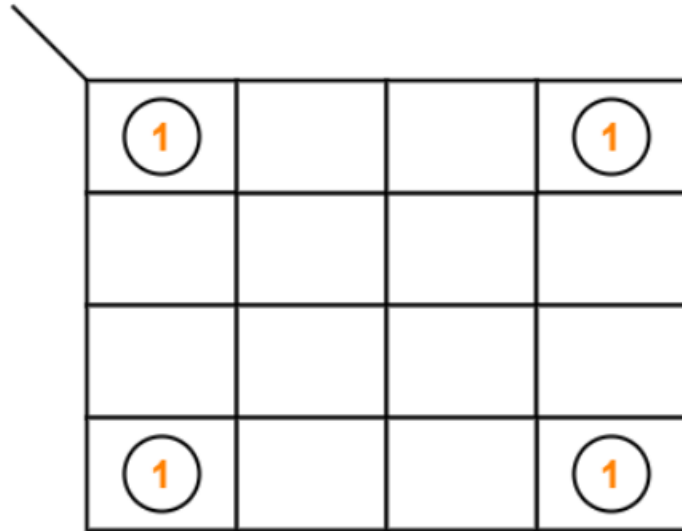
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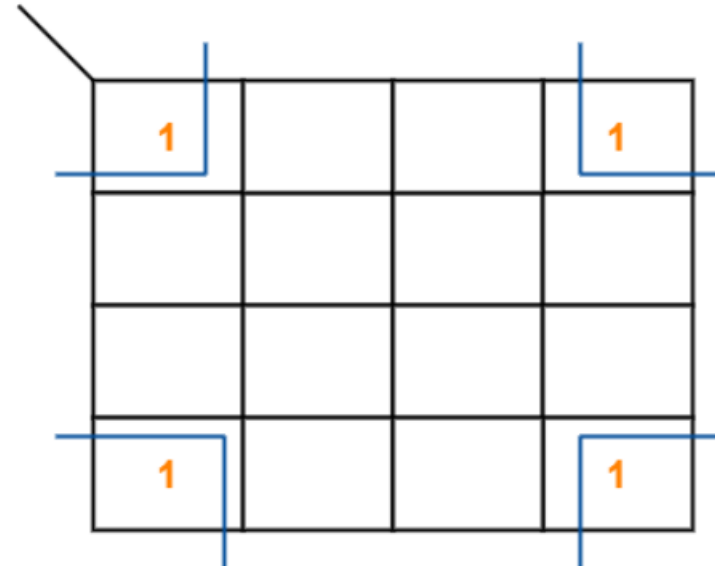
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WRONG PRACTICES IN GROUPING



Incorrect



Correct





Assessment

1. What is the necessity of K-Map?

2. Mention few methods used to minimize Boolean Expression?



*Thank
you*

